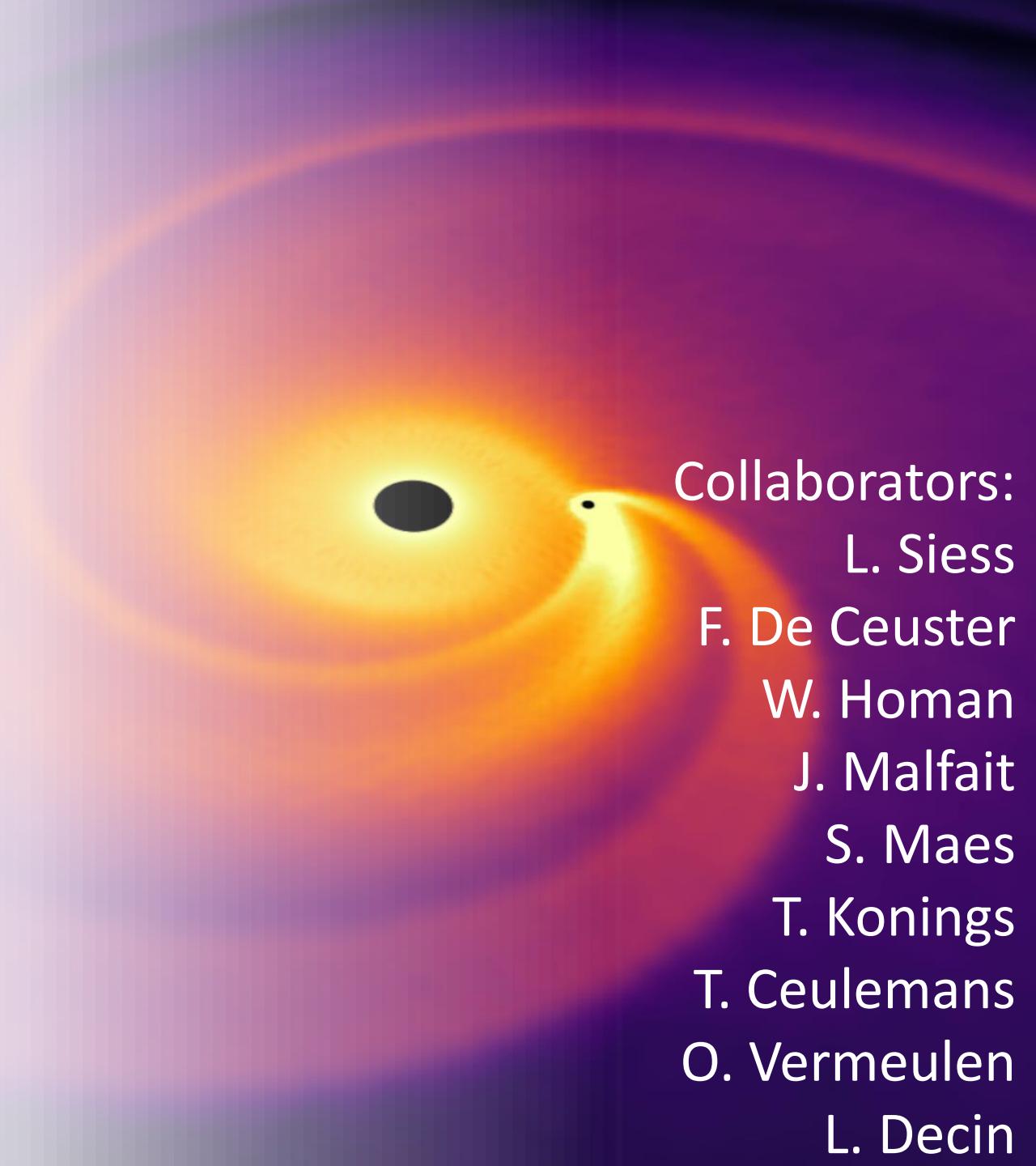


# Enhancing AGB Outflow Simulations: Implementing a Ray-Tracing Algorithm in PHANTOM for Efficient Radiation Field Computation

---

Mats Esseldeurs

Instituut voor sterrenkunde  
KU Leuven

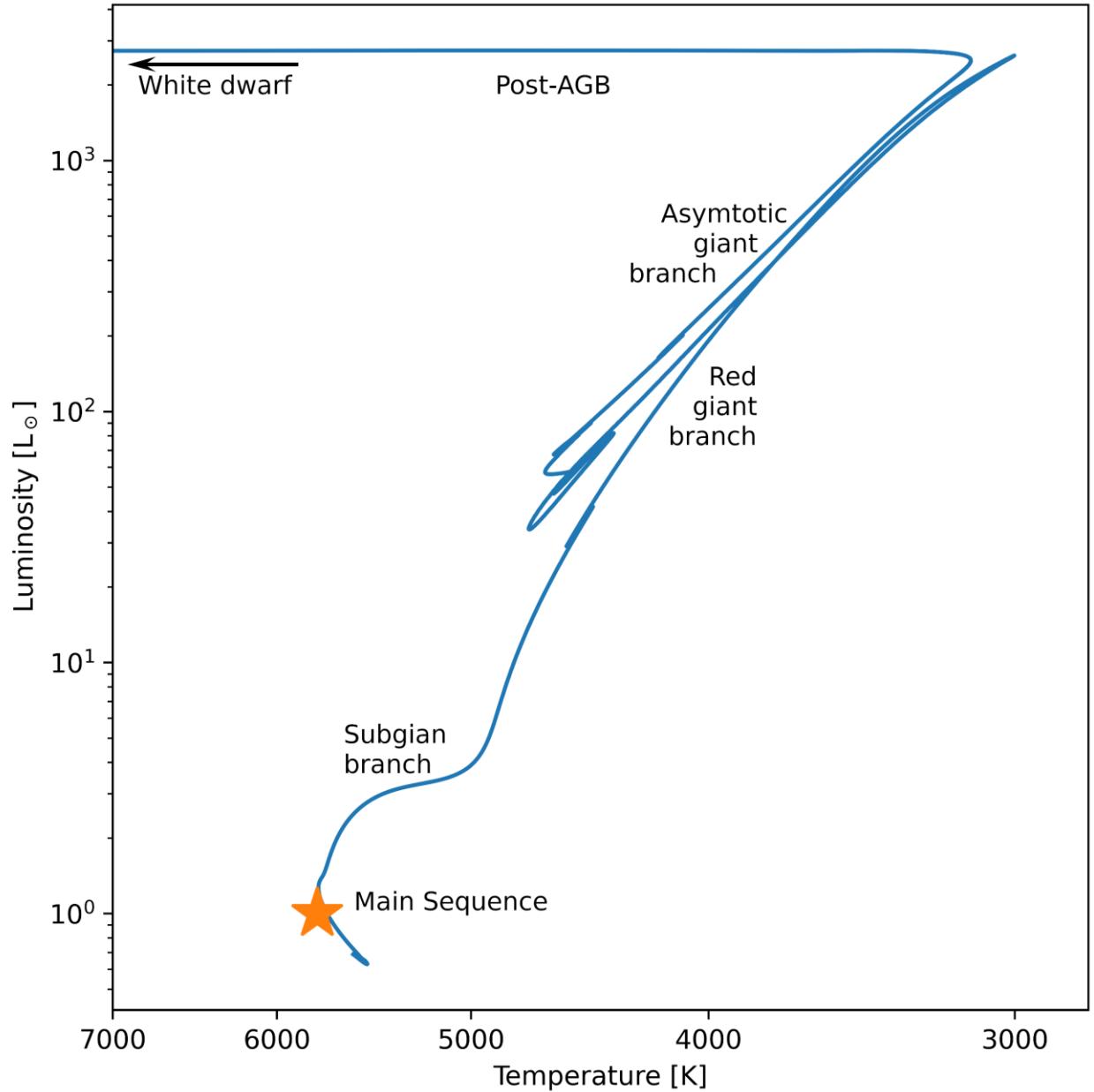


Collaborators:  
L. Siess  
F. De Ceuster  
W. Homan  
J. Malfait  
S. Maes  
T. Konings  
T. Ceulemans  
O. Vermeulen  
L. Decin

# AGB stars

- Low and intermediate mass
- $M_{ini} \in [0.8 M_{\odot}, 8 M_{\odot}]$

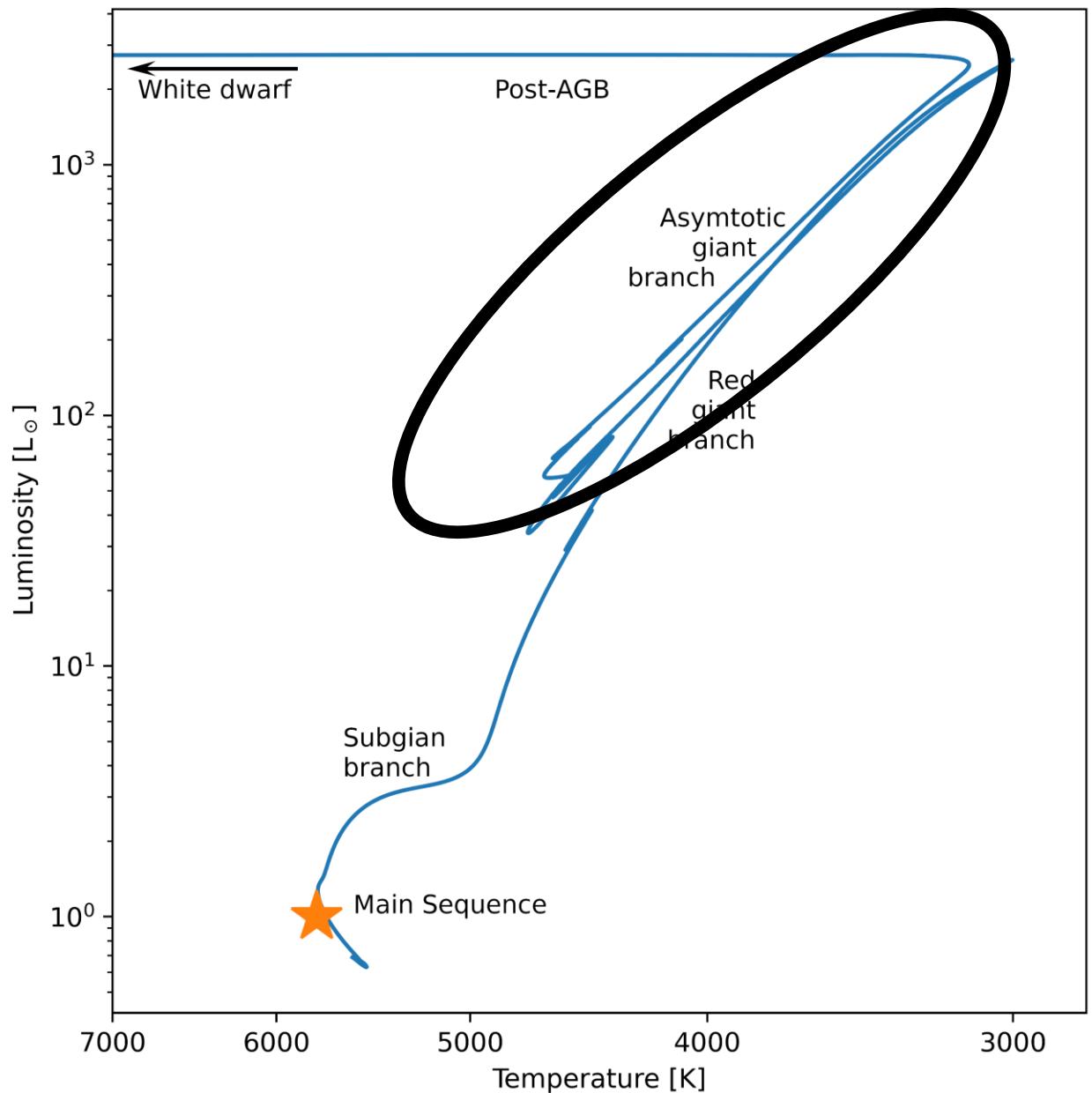
Evolution of  $1 M_{\odot}$  star



# AGB stars

- Low and intermediate mass
- $M_{ini} \in [0.8 M_{\odot}, 8 M_{\odot}]$

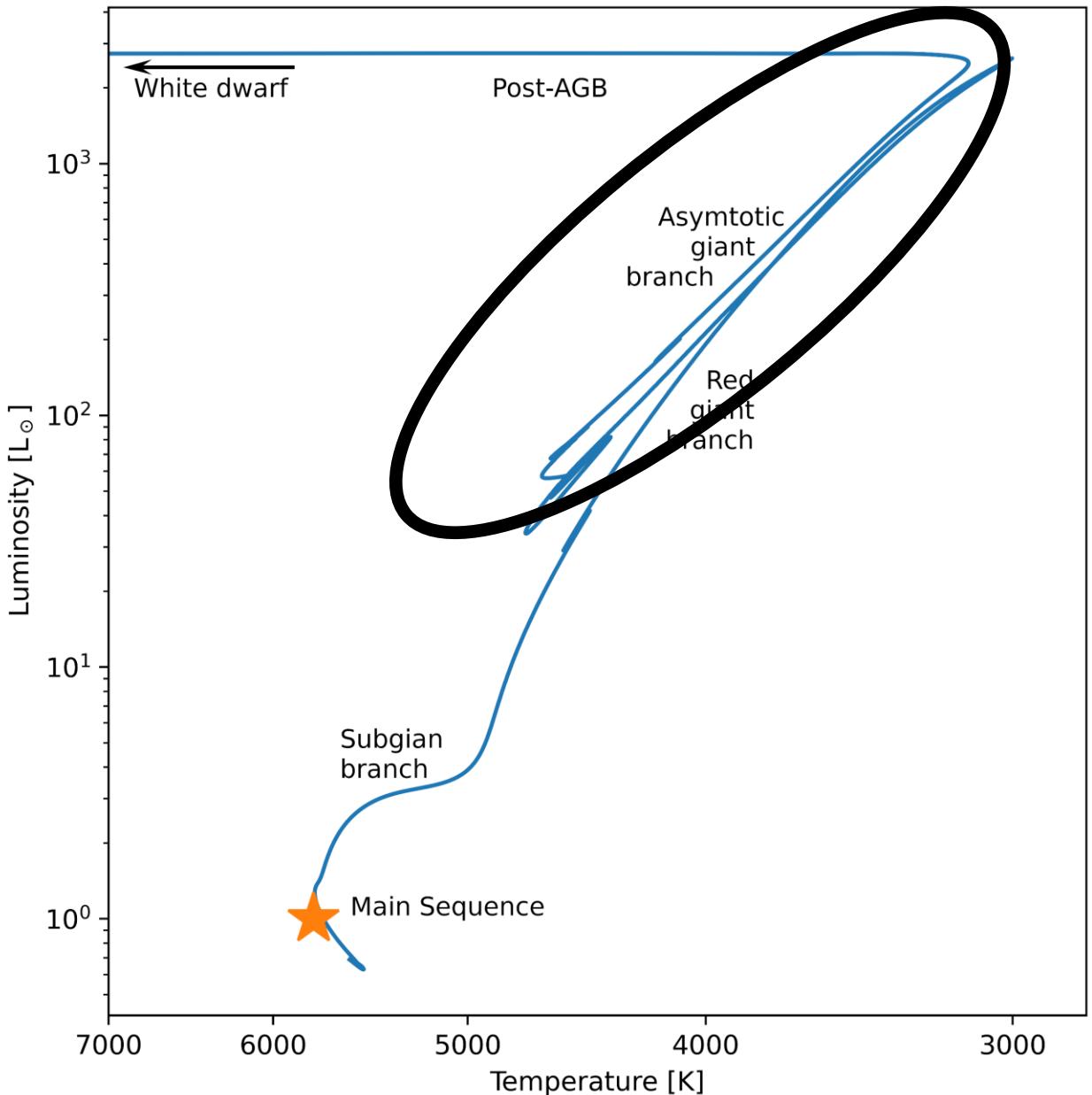
Evolution of  $1 M_{\odot}$  star



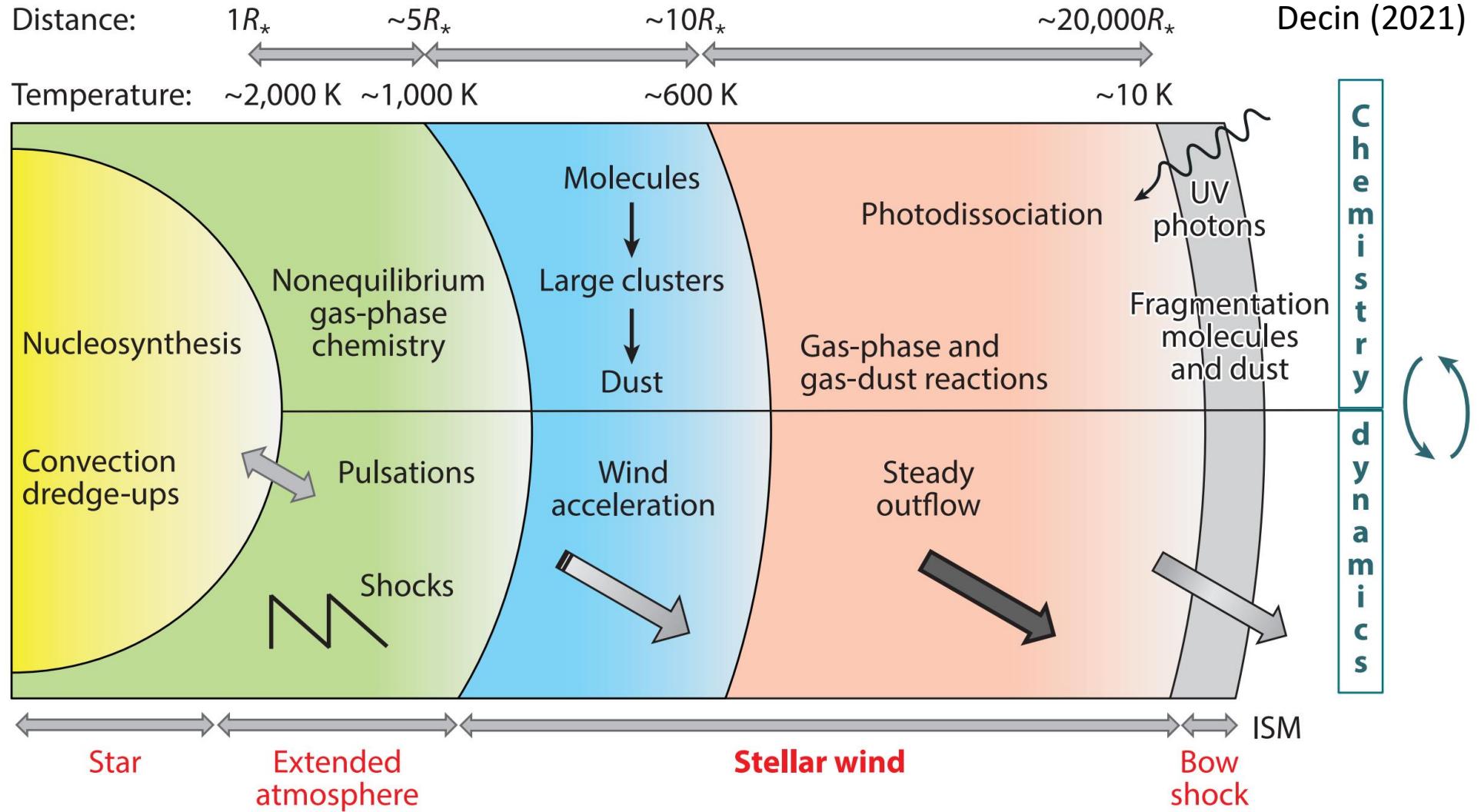
# AGB stars

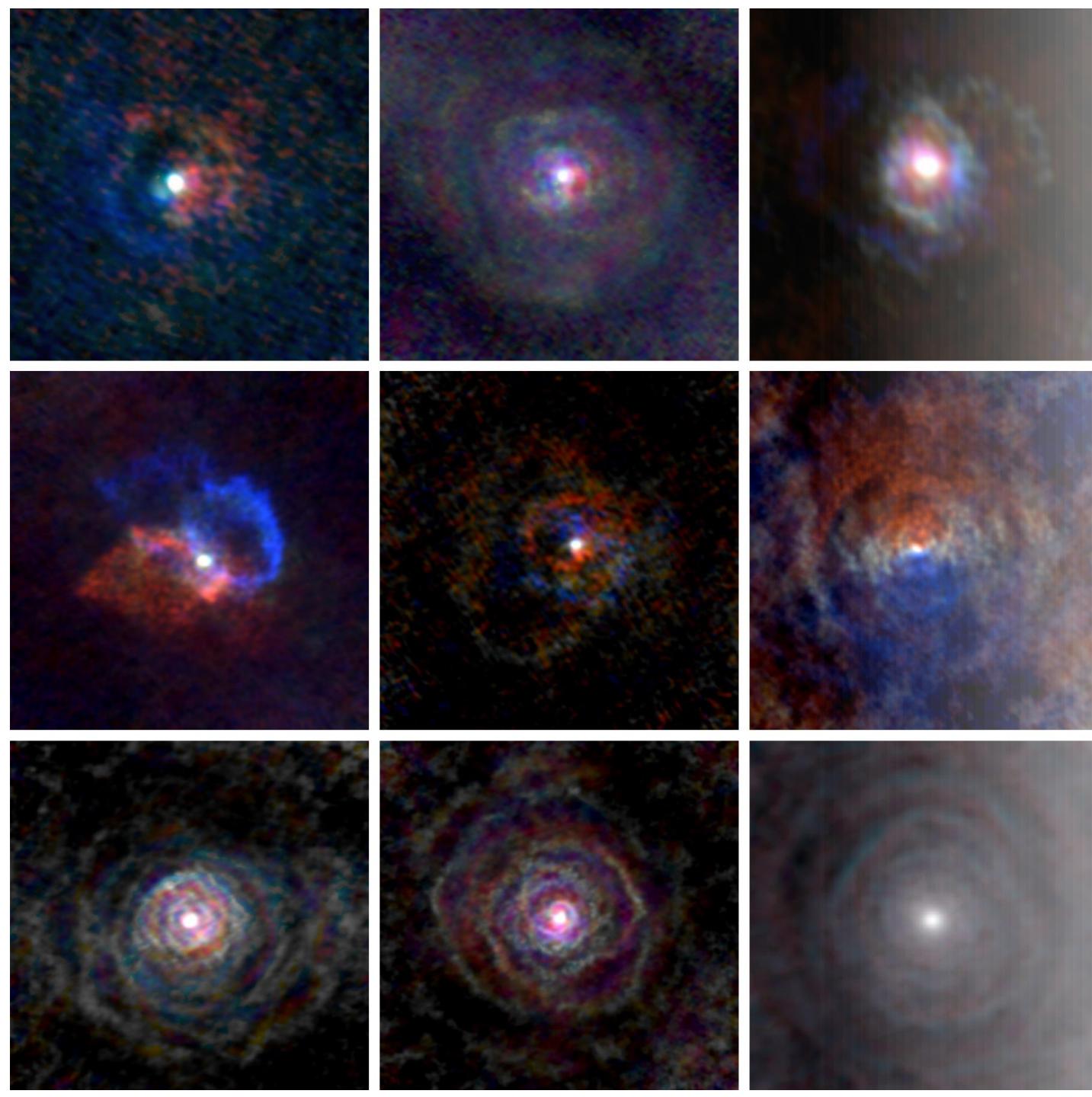
- Low and intermediate mass
- $M_{ini} \in [0.8 M_{\odot}, 8 M_{\odot}]$
- Significant mass loss
  - $\dot{M} = 10^{-8} - 10^{-4} M_{\odot}/\text{yr}$
  - $v_{\infty} = 5 - 25 \text{ km/s}$
- Dust-driven wind

Evolution of  $1 M_{\odot}$  star



# AGB's dust-driven wind





## AGB outflows

- Non-spherically symmetric
- Companion perturbed
- understanding through simulations

Decin et al. (2020)



# Hydrodynamic setup

- 3D Smoothed Particle Hydrodynamics (SPH)

- External acceleration

- $\vec{a} = -\frac{GM_{AGB}}{r_1^2}(1-\Gamma)\hat{r}_1 - \frac{GM_{comp}}{r_2^2}\hat{r}_2$



# Hydrodynamic setup

- 3D Smoothed Particle Hydrodynamics (SPH)

- External acceleration

$$\bullet \vec{a} = -\underbrace{\frac{GM_{AGB}}{r_1^2}}_{\text{Gravity AGB star}}(1-\Gamma)\hat{r}_1 - \frac{GM_{comp}}{r_2^2}\hat{r}_2$$



# Hydrodynamic setup

- 3D Smoothed Particle Hydrodynamics (SPH)

- External acceleration

$$\vec{a} = - \underbrace{\frac{GM_{AGB}}{r_1^2}}_{\text{Gravity AGB star}} (1 - \Gamma) \hat{r}_1 - \underbrace{\frac{GM_{comp}}{r_2^2}}_{\text{Gravity companion}} \hat{r}_2$$



# Hydrodynamic setup

- 3D Smoothed Particle Hydrodynamics (SPH)

- External acceleration

$$\vec{a} = - \underbrace{\frac{GM_{AGB}}{r_1^2}}_{\substack{\text{Gravity} \\ \text{AGB star}}} (1 - \Gamma) \hat{r}_1 - \underbrace{\frac{GM_{comp}}{r_2^2}}_{\substack{\text{Gravity} \\ \text{companion}}} \hat{r}_2$$

wind launching



# Hydrodynamic setup

- 3D Smoothed Particle Hydrodynamics (SPH)

- External acceleration

$$\bullet \vec{a} = -\underbrace{\frac{GM_{AGB}}{r_1^2}(1-\Gamma)\hat{r}_1}_{\begin{array}{c} \text{Gravity} \\ \text{AGB star} \end{array}} - \underbrace{\frac{GM_{comp}}{r_2^2}\hat{r}_2}_{\begin{array}{c} \text{Gravity} \\ \text{companion} \end{array}}, \quad \Gamma = 1$$

wind launching



# Hydrodynamic setup

- 3D Smoothed Particle Hydrodynamics (SPH)

- External acceleration

$$\vec{a} = - \underbrace{\frac{GM_{AGB}}{r_1^2}}_{\substack{\text{Gravity} \\ \text{AGB star}}} (1 - \Gamma) \hat{r}_1 - \underbrace{\frac{GM_{comp}}{r_2^2} \hat{r}_2}_{\substack{\text{Gravity} \\ \text{companion}}} , \quad \cancel{\Gamma}$$

- Eddington factor: radiative acceleration

$$\bullet \quad \Gamma = \frac{\kappa F/c}{GM_{AGB}/r_1^2}, \quad \kappa(T_{eq}) = \frac{\kappa_{max}}{1 + \exp[(T_{eq} - T_{cond})/\delta]} + \kappa_g$$



# Hydrodynamic setup

- 3D Smoothed Particle Hydrodynamics (SPH)

- External acceleration

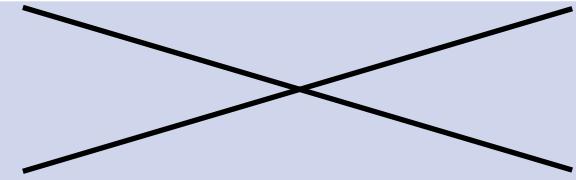
$$\vec{a} = - \underbrace{\frac{GM_{AGB}}{r_1^2}}_{\substack{\text{Gravity} \\ \text{AGB star}}} (1 - \Gamma) \hat{r}_1 - \underbrace{\frac{GM_{comp}}{r_2^2} \hat{r}_2}_{\substack{\text{Gravity} \\ \text{companion}}} , \quad \cancel{\Gamma}$$

- Eddington factor: radiative acceleration

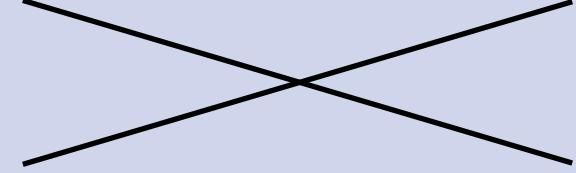
$$\Gamma = \frac{\kappa F/c}{GM_{AGB}/r_1^2}, \quad \kappa(T_{eq}) = \frac{\kappa_{max}}{1 + \exp[(T_{eq} - T_{cond})/\delta]} + \kappa_g$$



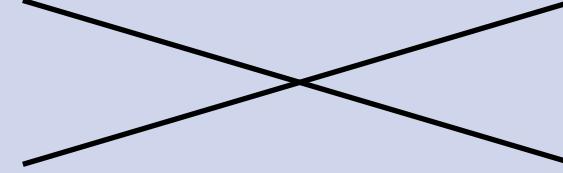
# Approximations

Approximations	$\Gamma$	$T_{eq}$
Free-wind	$\Gamma = 1$	

# Approximations

Approximations	$\Gamma$	$T_{eq}$
Free-wind	$\Gamma = 1$	
Geometrical	$\Gamma = \frac{\kappa L_{AGB}}{4\pi c G M_{AGB}}$	$T_{eq}^4 = \frac{1}{2} \left( 1 - \sqrt{1 - \left(\frac{R_\star}{r}\right)^2} \right) T_\star^4$

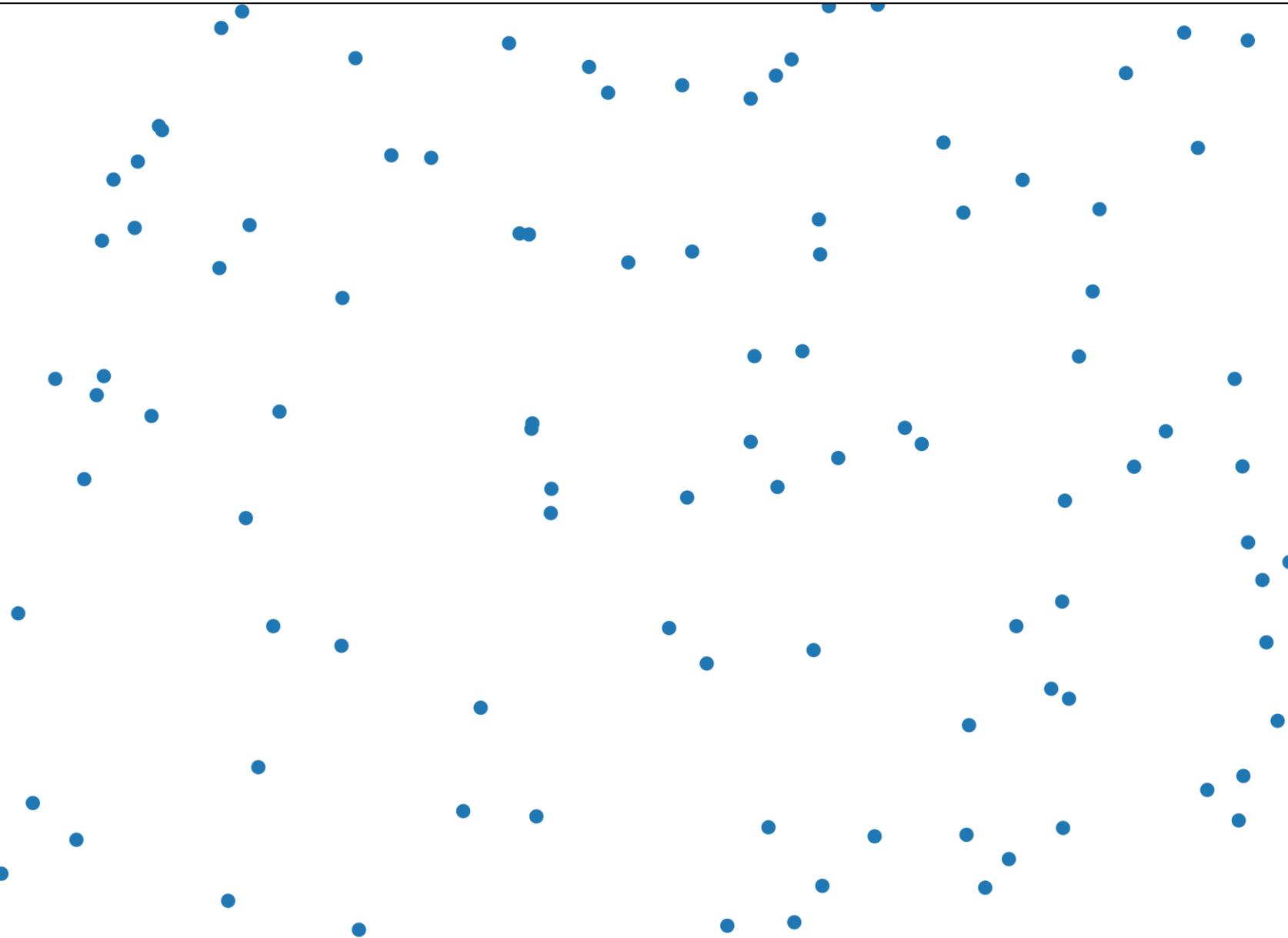
# Approximations

Approximations	$\Gamma$	$T_{eq}$
Free-wind	$\Gamma = 1$	
Geometrical	$\Gamma = \frac{\kappa L_{AGB}}{4\pi c G M_{AGB}}$	$T_{eq}^4 = \frac{1}{2} \left( 1 - \sqrt{1 - \left(\frac{R_\star}{r}\right)^2} \right) T_\star^4$
Lucy	$\Gamma = \frac{\kappa L_{AGB}}{4\pi c G M_{AGB}}$	$T_{eq}^4 = \frac{1}{2} \left( 1 - \sqrt{1 - \left(\frac{R_\star}{r}\right)^2} + \frac{2}{3} \tau_L \right) T_\star^4$

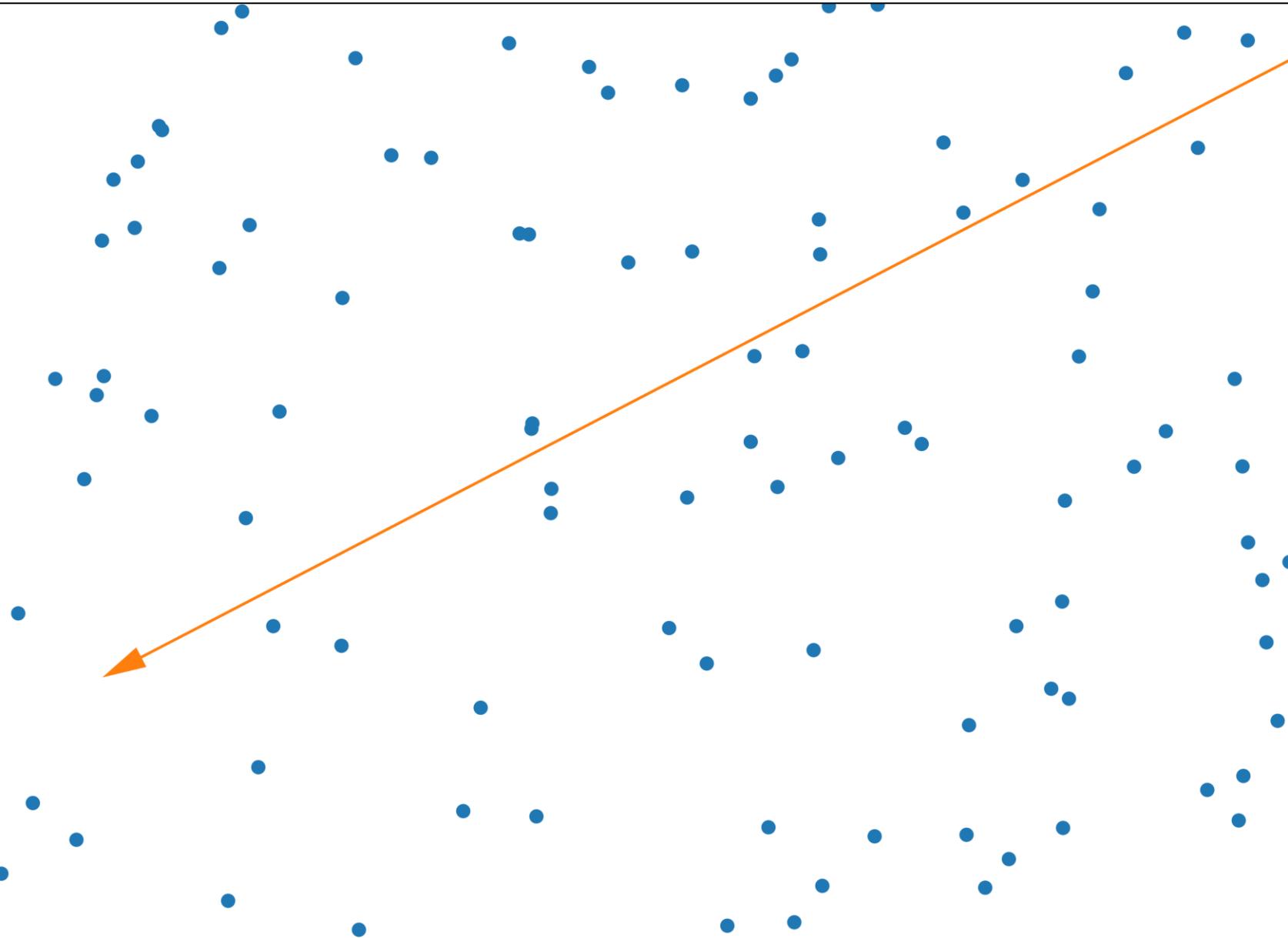
# Approximations

Approximations	$\Gamma$	$T_{eq}$
Free-wind	$\Gamma = 1$	
Geometrical	$\Gamma = \frac{\kappa L_{AGB}}{4\pi c G M_{AGB}}$	$T_{eq}^4 = \frac{1}{2} \left( 1 - \sqrt{1 - \left(\frac{R_\star}{r}\right)^2} \right) T_\star^4$
Lucy	$\Gamma = \frac{\kappa L_{AGB}}{4\pi c G M_{AGB}}$	$T_{eq}^4 = \frac{1}{2} \left( 1 - \sqrt{1 - \left(\frac{R_\star}{r}\right)^2} + \frac{2}{3} \tau_L \right) T_\star^4$
Attenuation	$\Gamma = \frac{\kappa L_{AGB}}{4\pi c G M_{AGB}} e^{-\tau}$	$T_{eq}^4 = \frac{1}{2} \left( 1 - \sqrt{1 - \left(\frac{R_\star}{r}\right)^2} \right) e^{-\tau} T_\star^4$

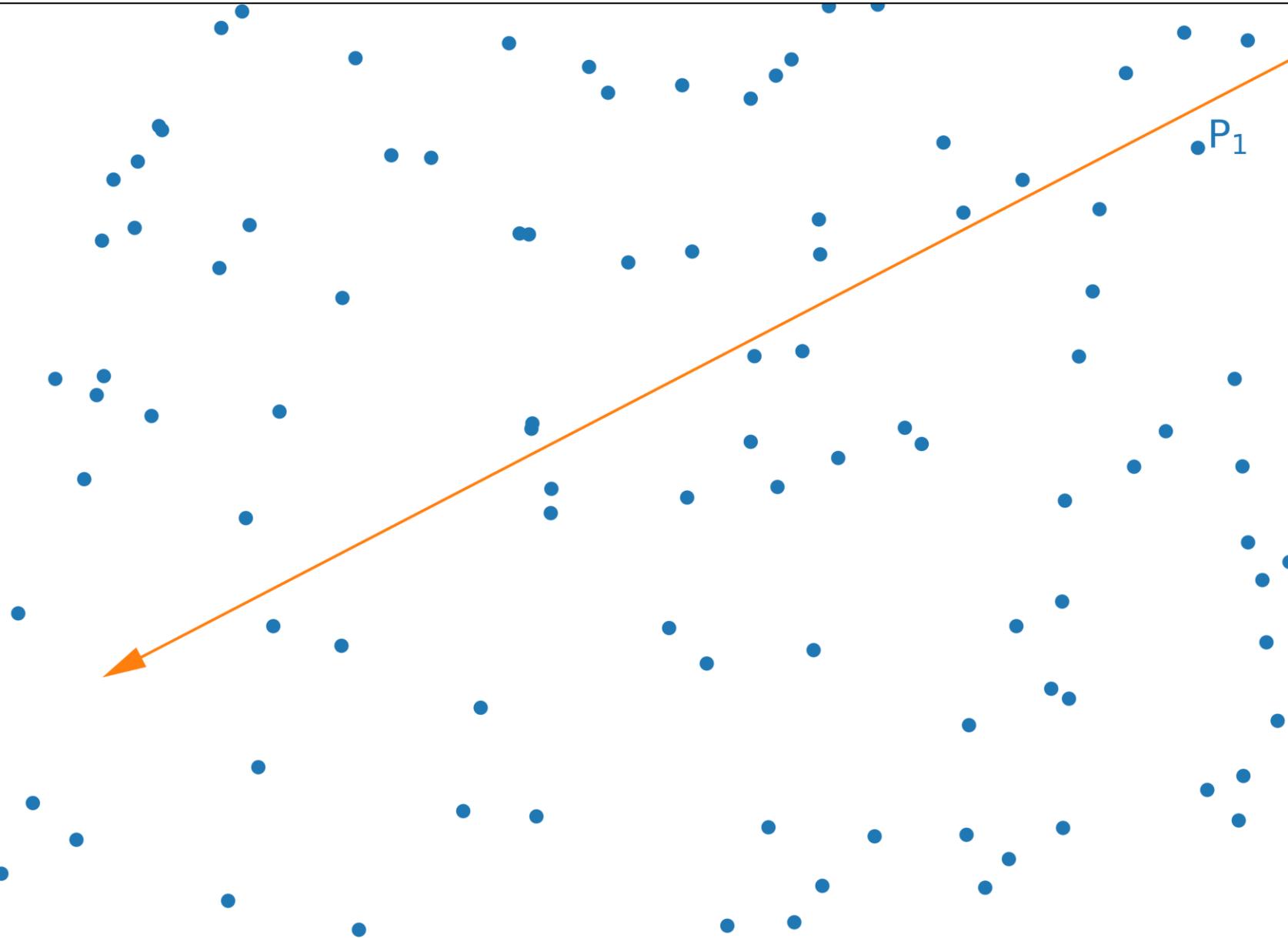
# Ray-tracer



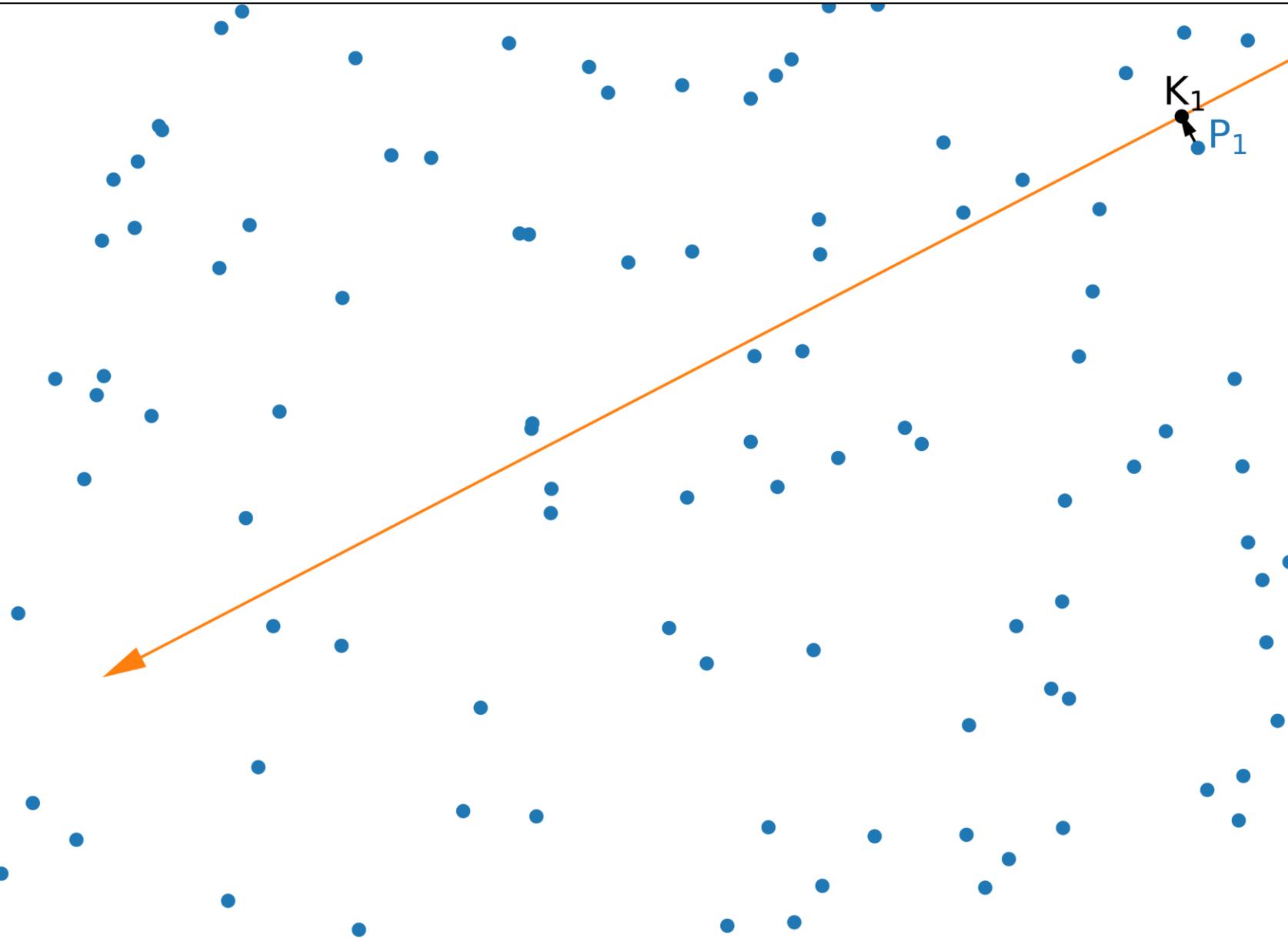
# Ray-tracer



# Ray-tracer



# Ray-tracer

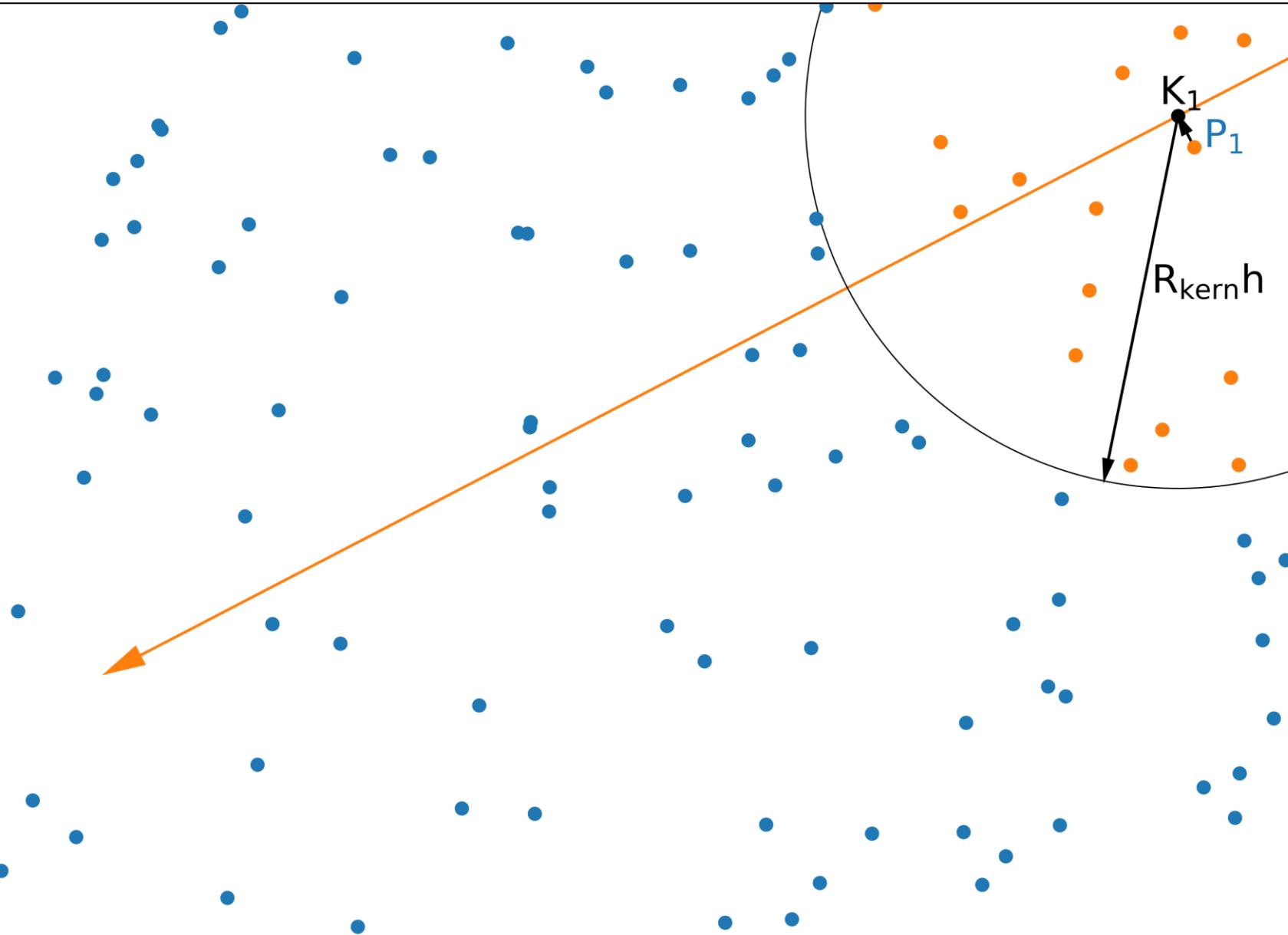


# Ray-tracer



At each point K:

- $K_i \rho_i$
- $d_i$

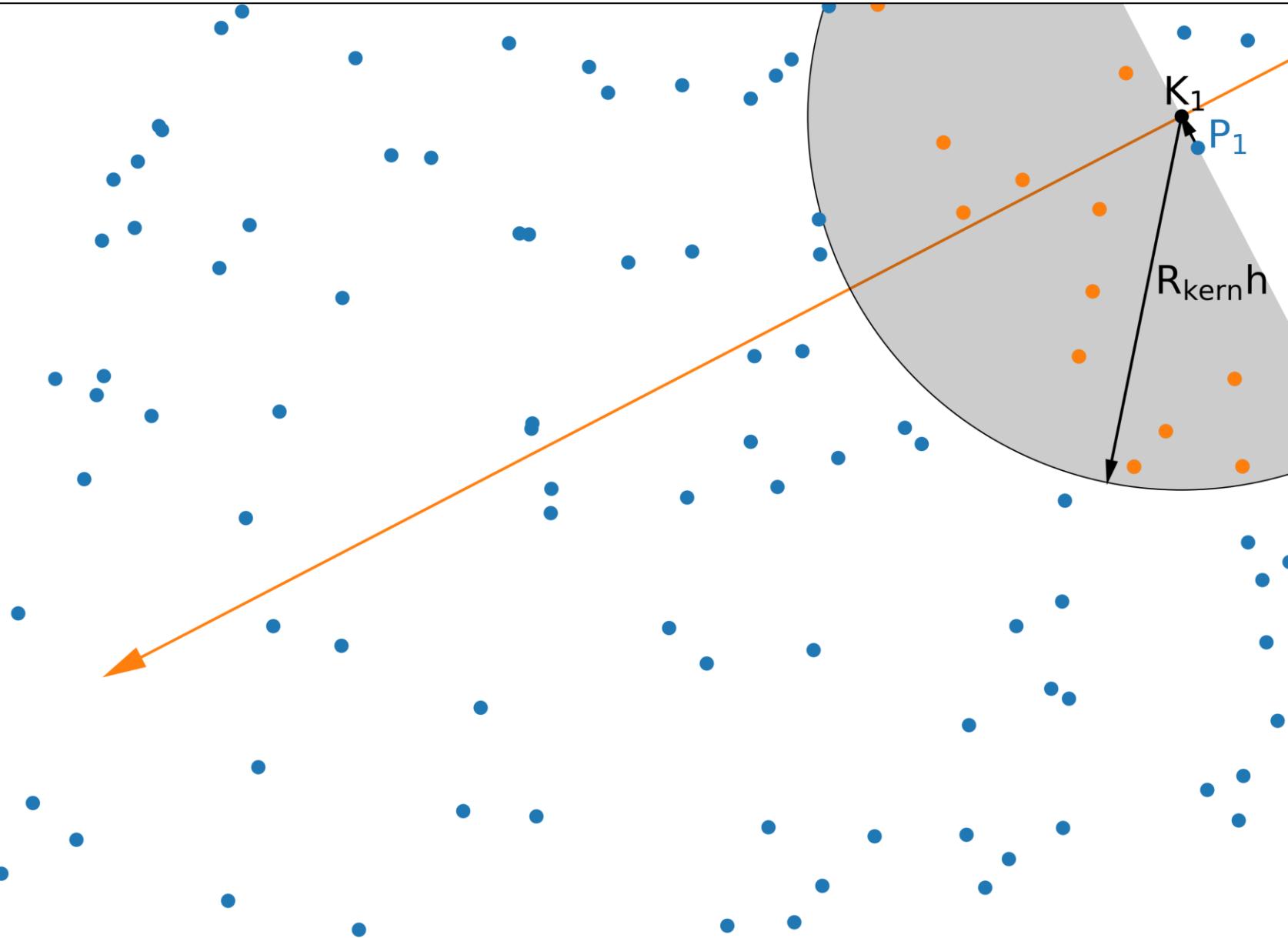


# Ray-tracer



At each point K:

- $K_i \rho_i$
- $d_i$

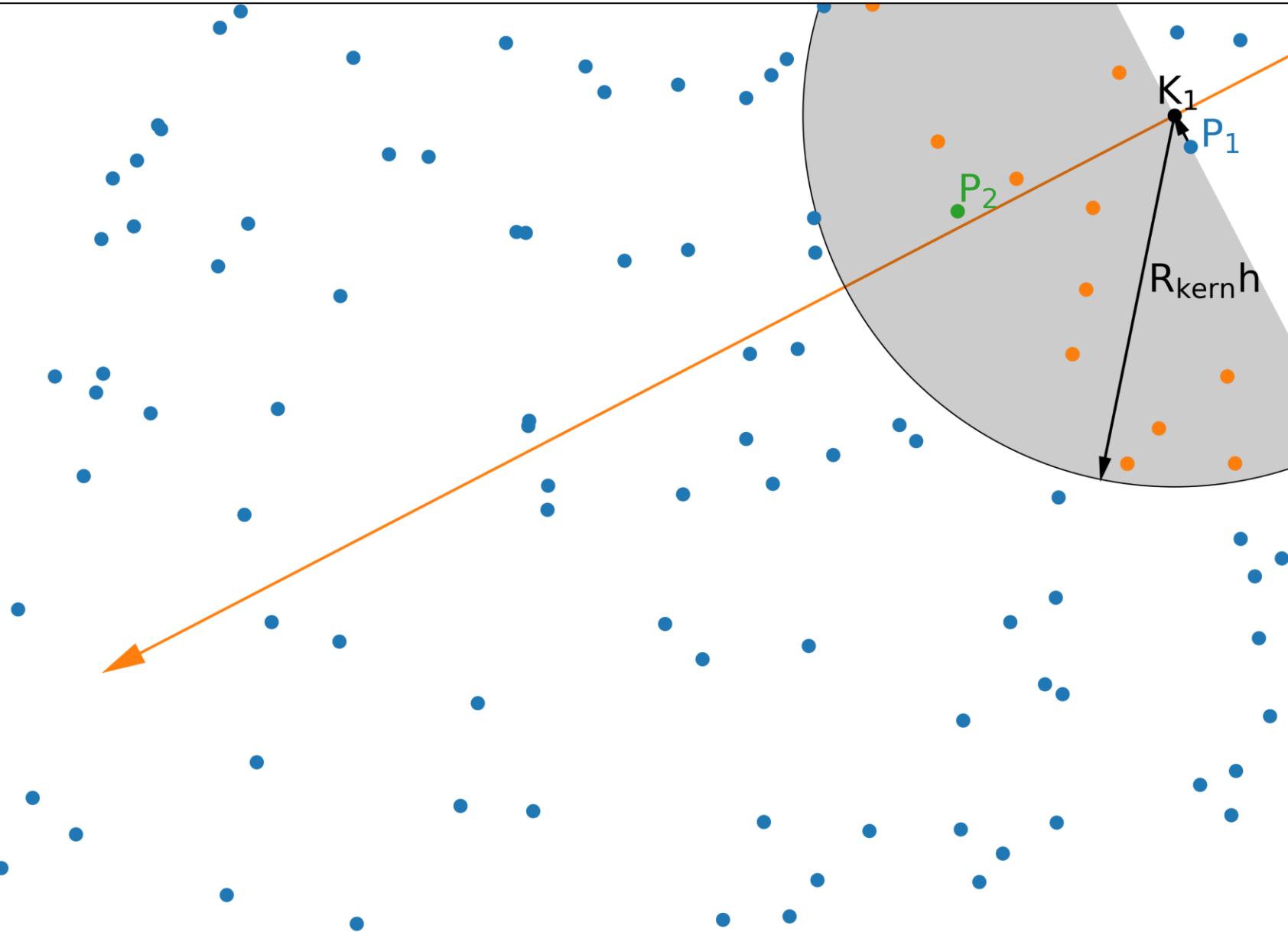


# Ray-tracer



At each point K:

- $K_i \rho_i$
- $d_i$

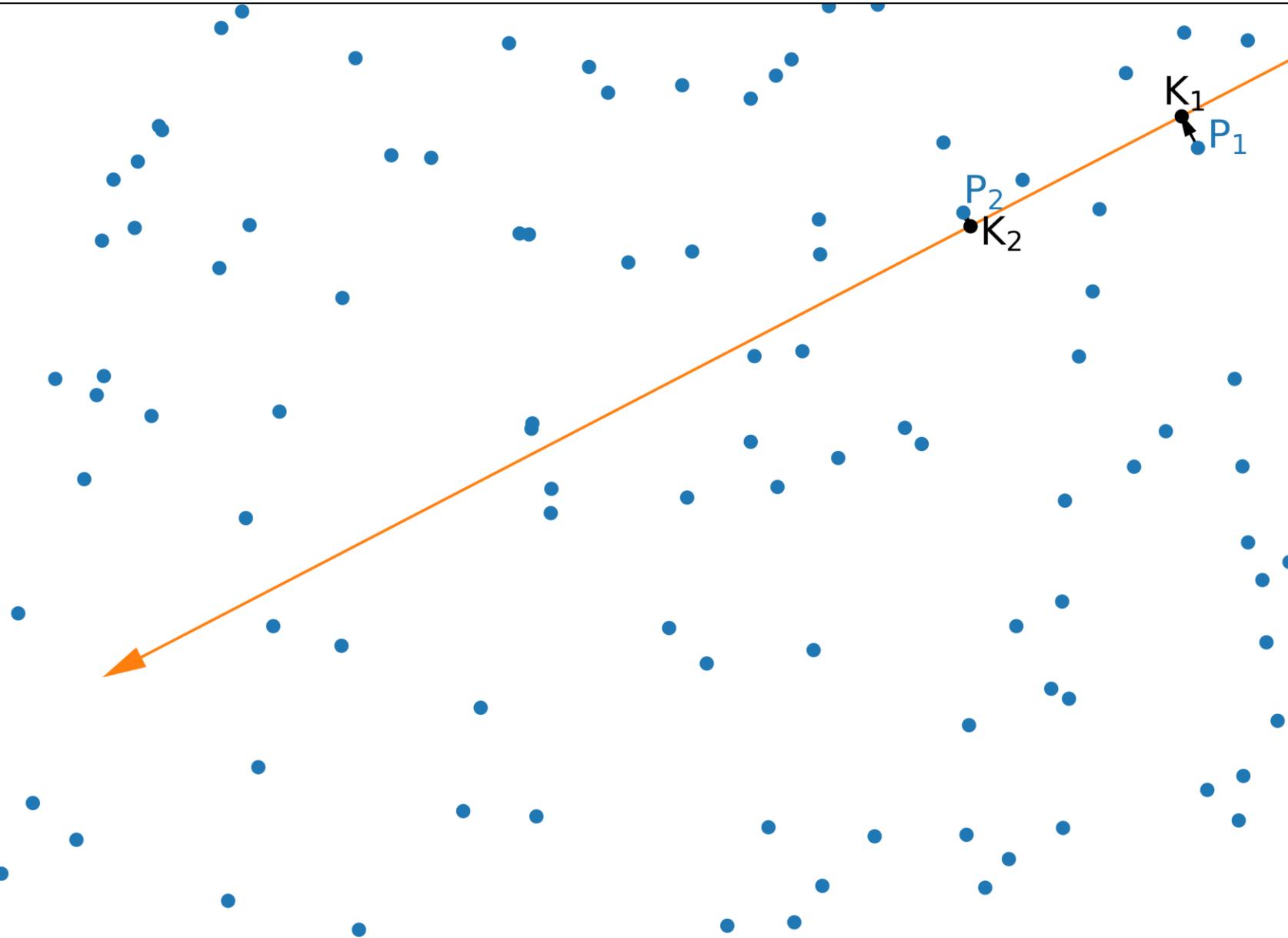


# Ray-tracer



At each point K:

- $K_i \rho_i$
- $d_i$

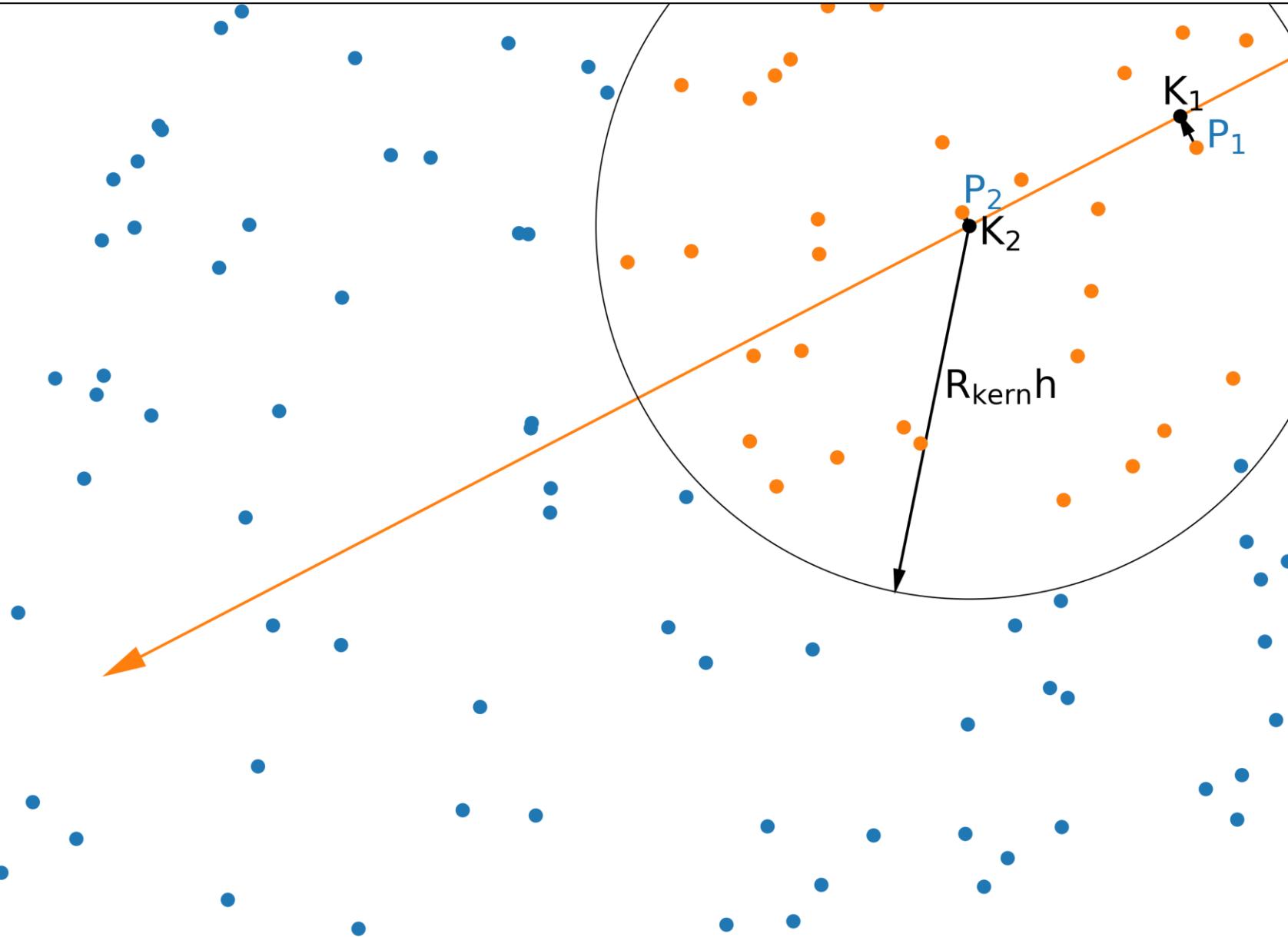


# Ray-tracer



At each point K:

- $K_i \rho_i$
- $d_i$

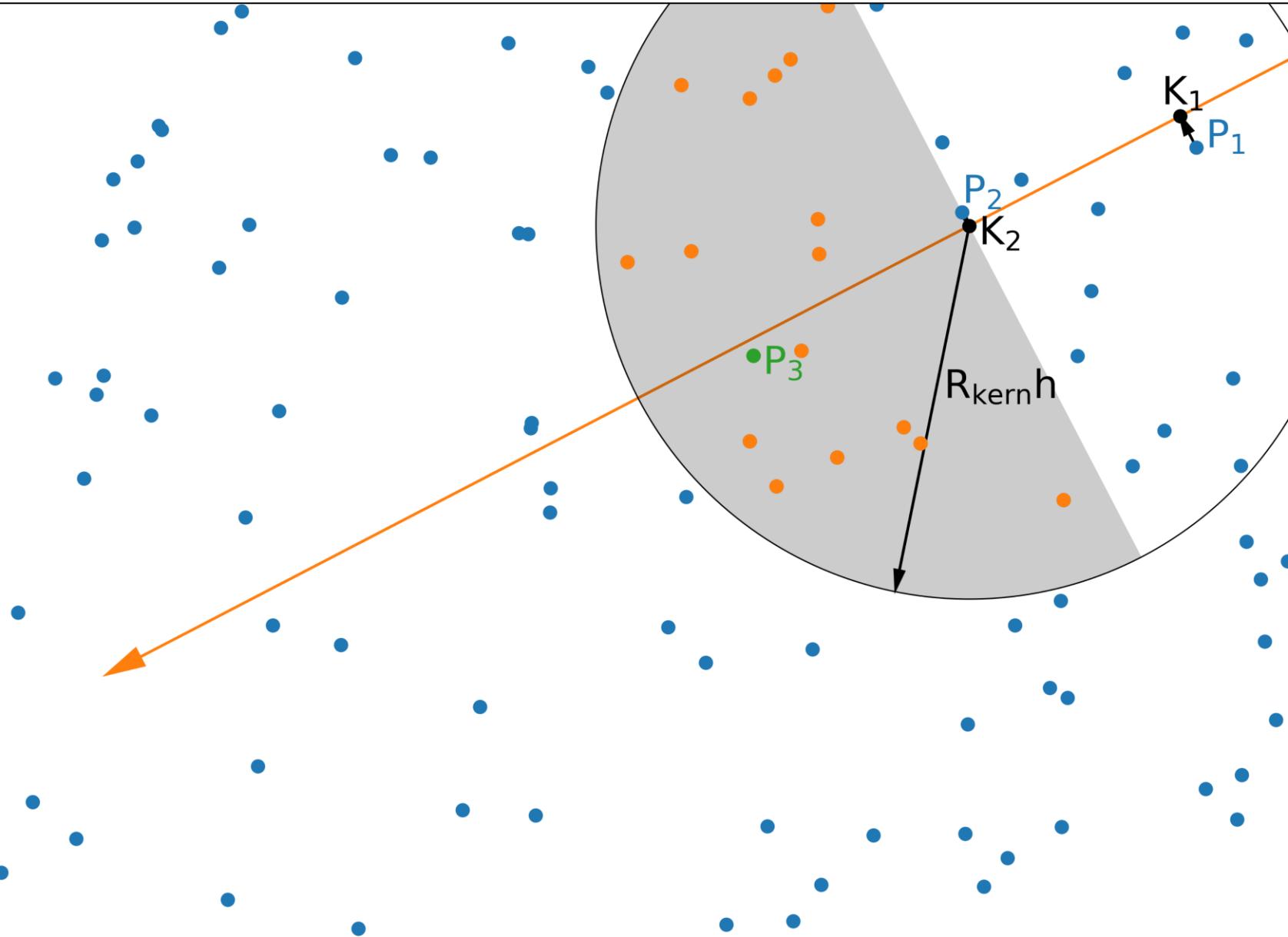


# Ray-tracer



At each point K:

- $K_i \rho_i$
- $d_i$

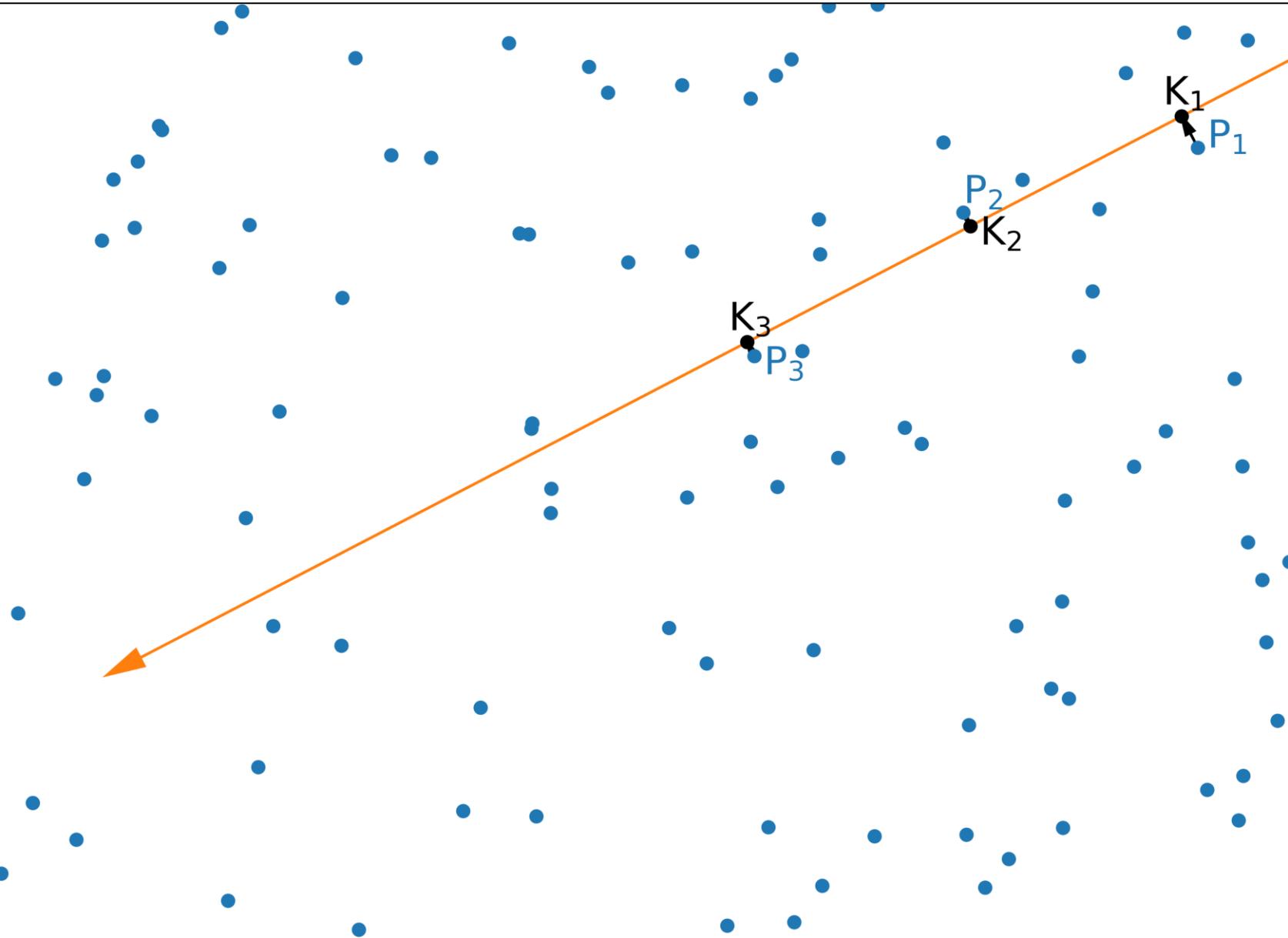


# Ray-tracer



At each point K:

- $K_i \rho_i$
- $d_i$

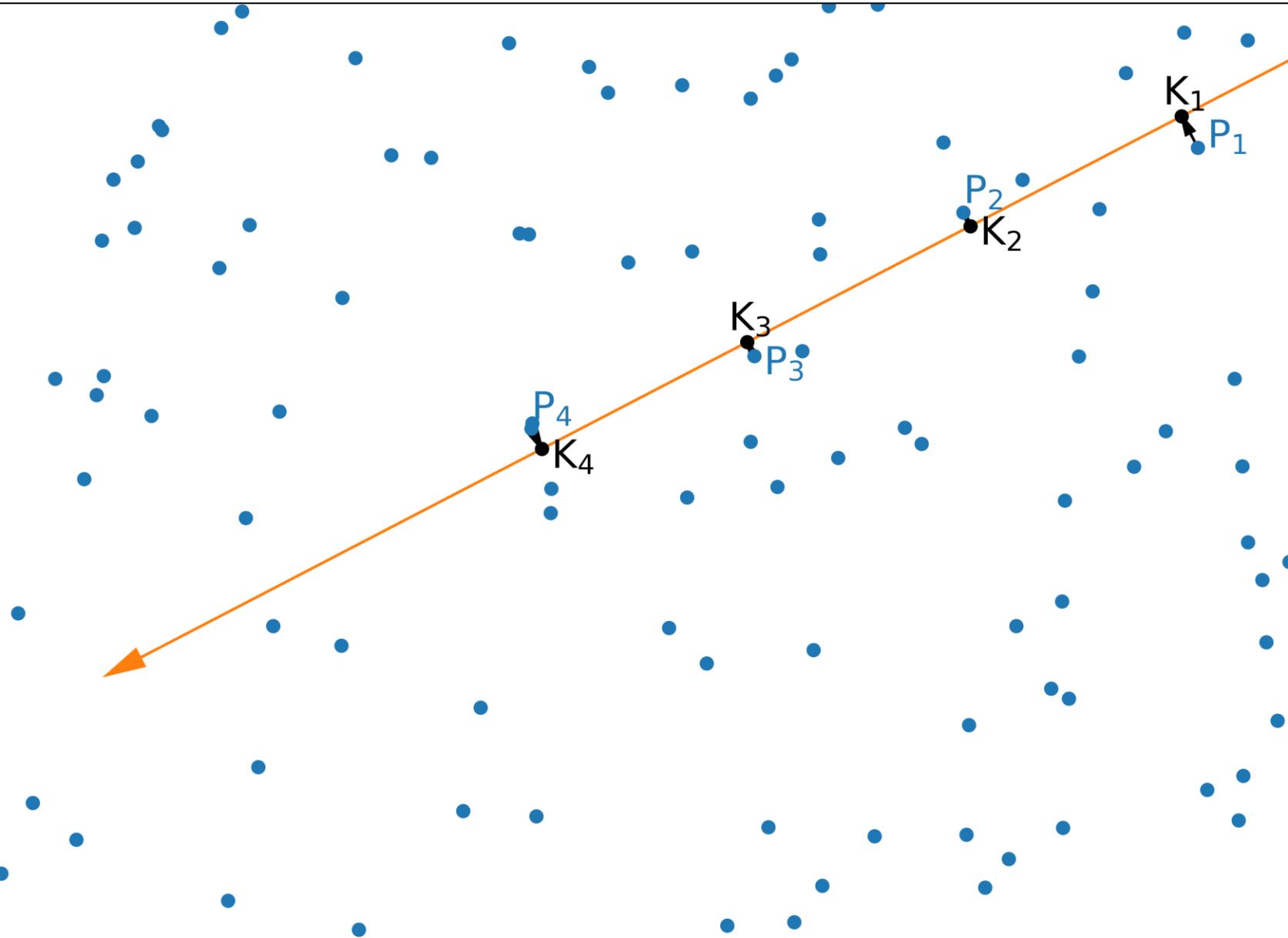


# Ray-tracer



At each point K:

- $K_i \rho_i$
- $d_i$

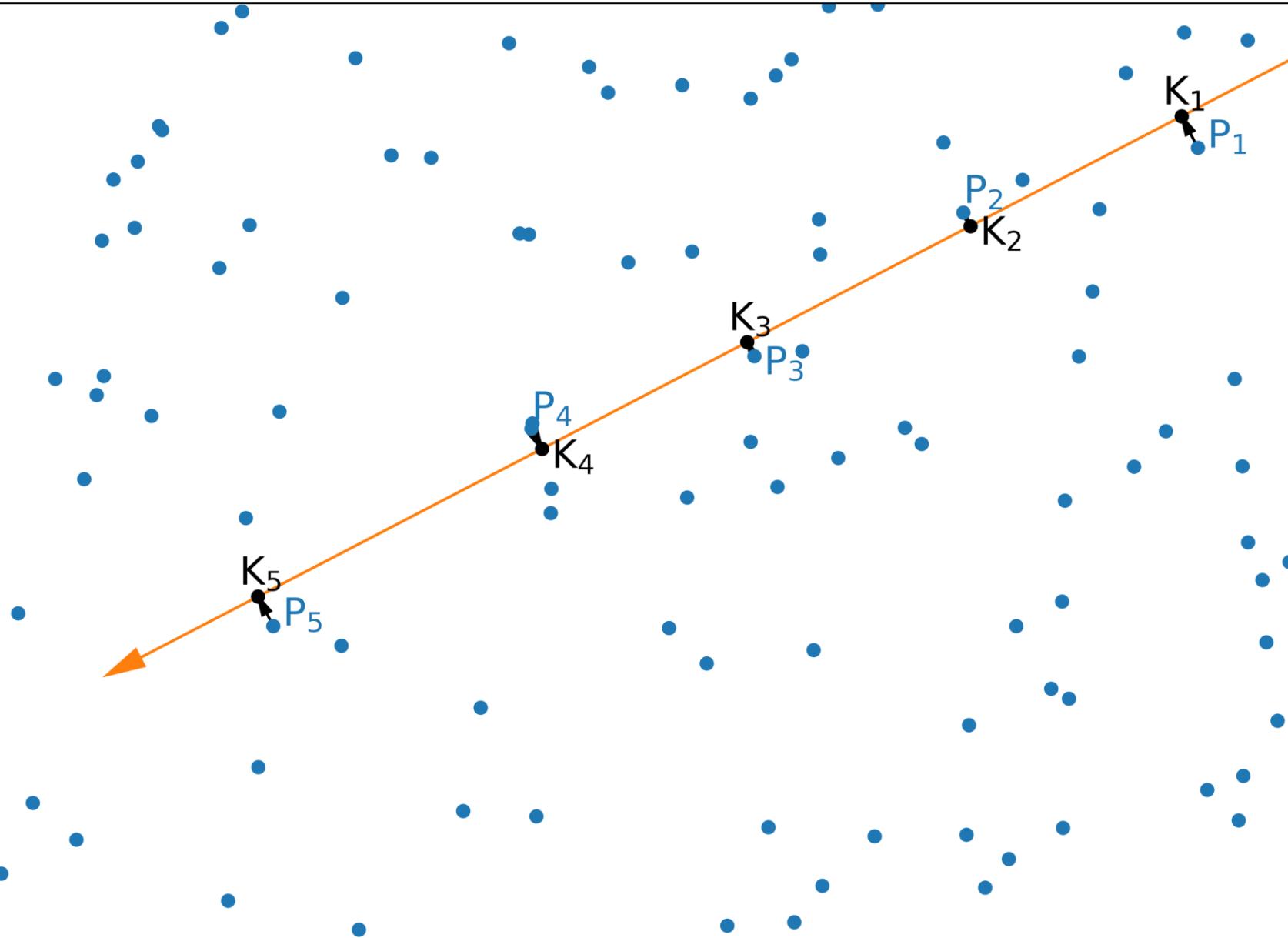


# Ray-tracer

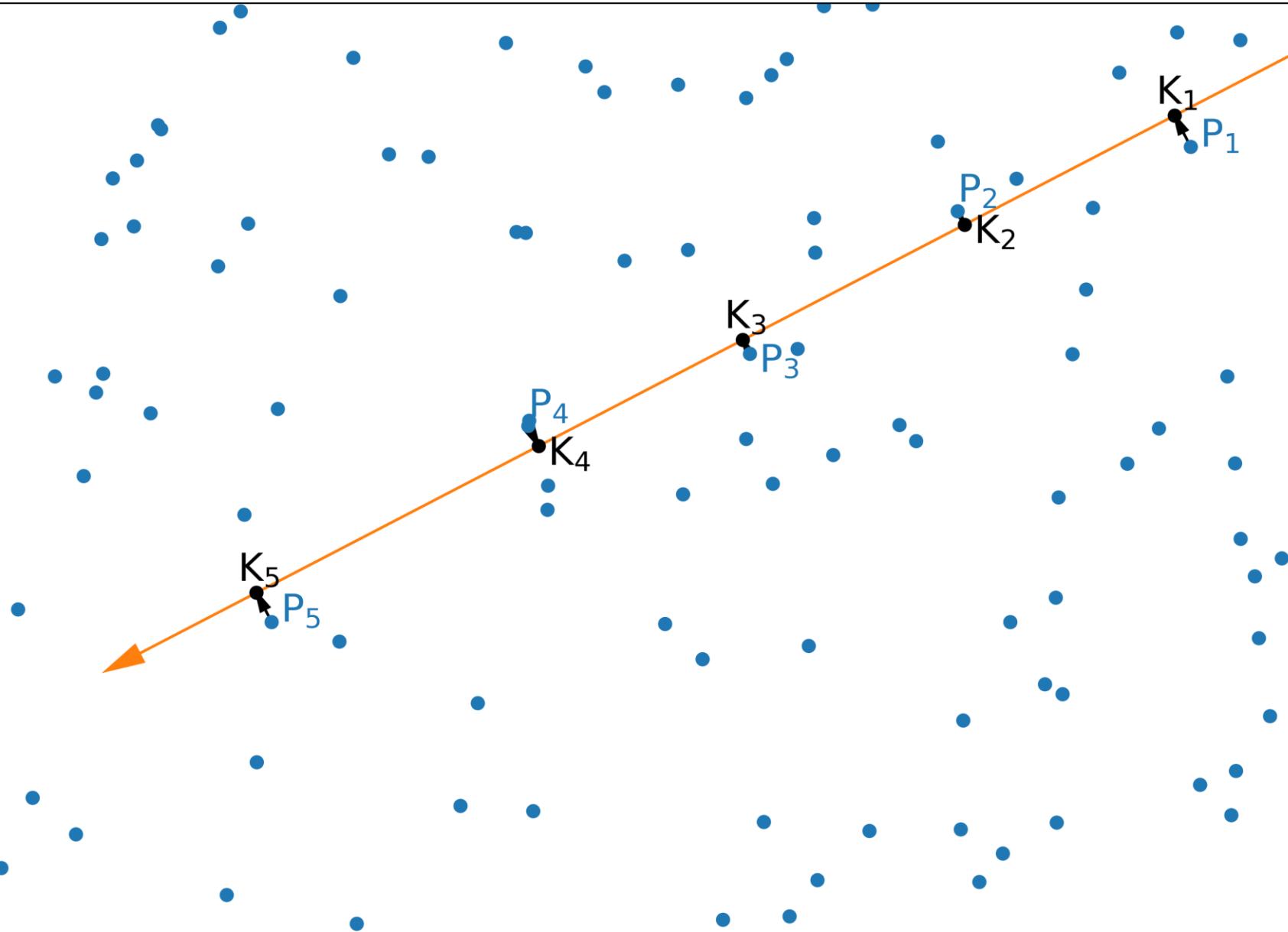


At each point K:

- $k_i \rho_i$
- $d_i$



# Ray-tracer

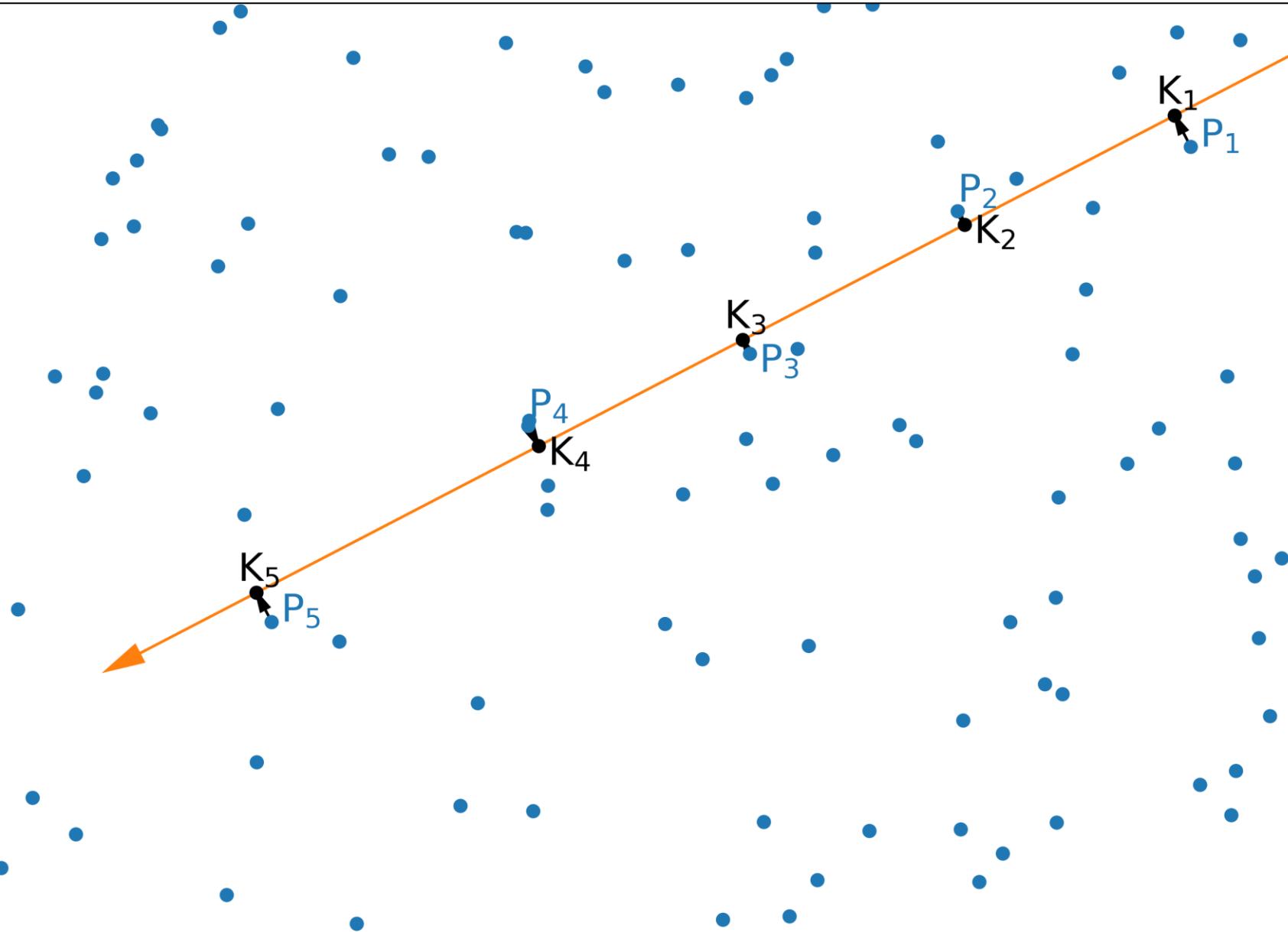


At each point K:

- $\kappa_i \rho_i$
- $d_i$

$$\begin{aligned}\tau &= \int_{R_*}^r d\tau \approx \sum_i \Delta\tau_i \\ &= \sum_i \left( \frac{\kappa_i \rho_i + \kappa_{i+1} \rho_{i+1}}{2} \right) \Delta s_i\end{aligned}$$

# Ray-tracer



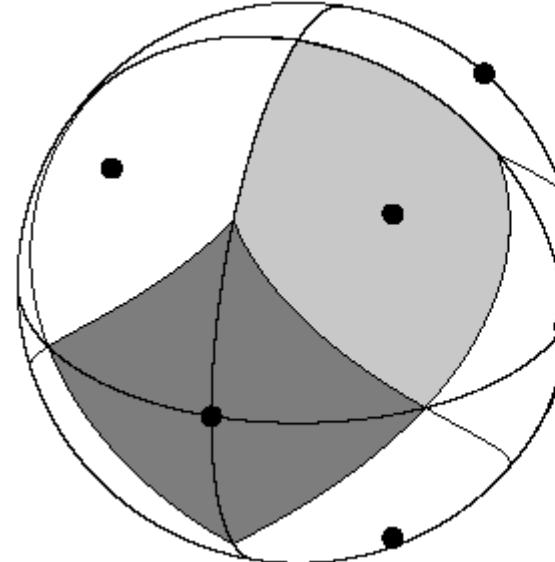
At each point K:

- $\kappa_i \rho_i$
- $d_i$
- $\tau_i$

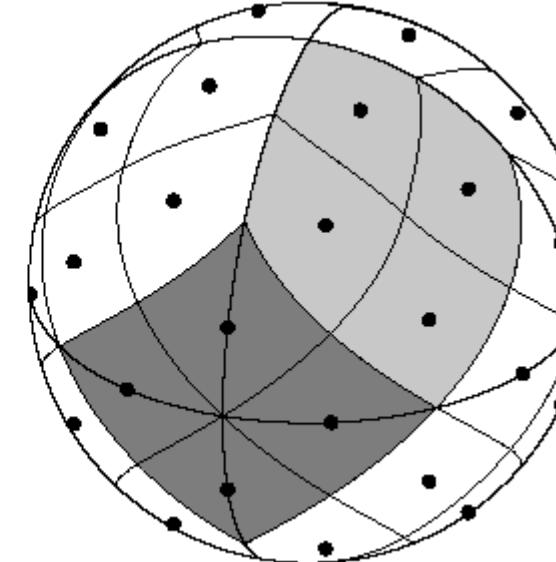
$$\begin{aligned}\tau &= \int_{R_*}^r d\tau \approx \sum_i \Delta\tau_i \\ &= \sum_i \left( \frac{\kappa_i \rho_i + \kappa_{i+1} \rho_{i+1}}{2} \right) \Delta s_i\end{aligned}$$

3D → Healpix

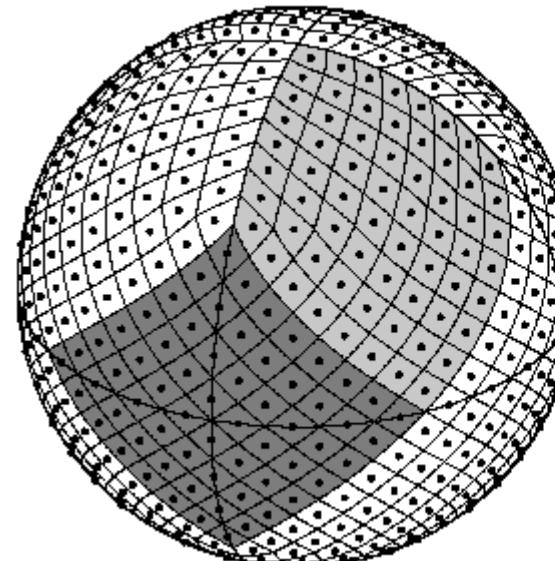
Order 0



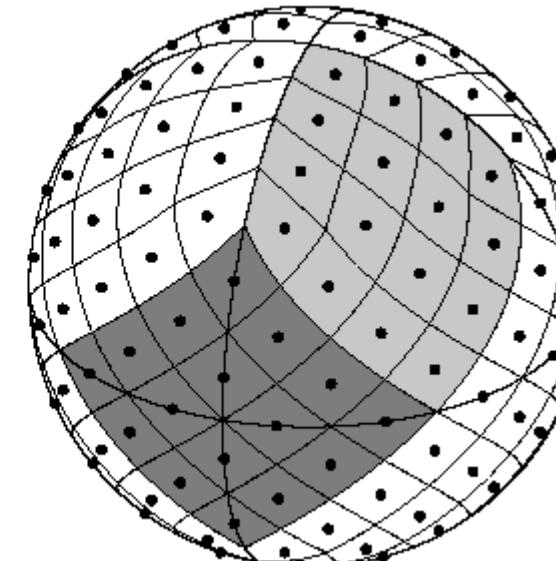
Order 1



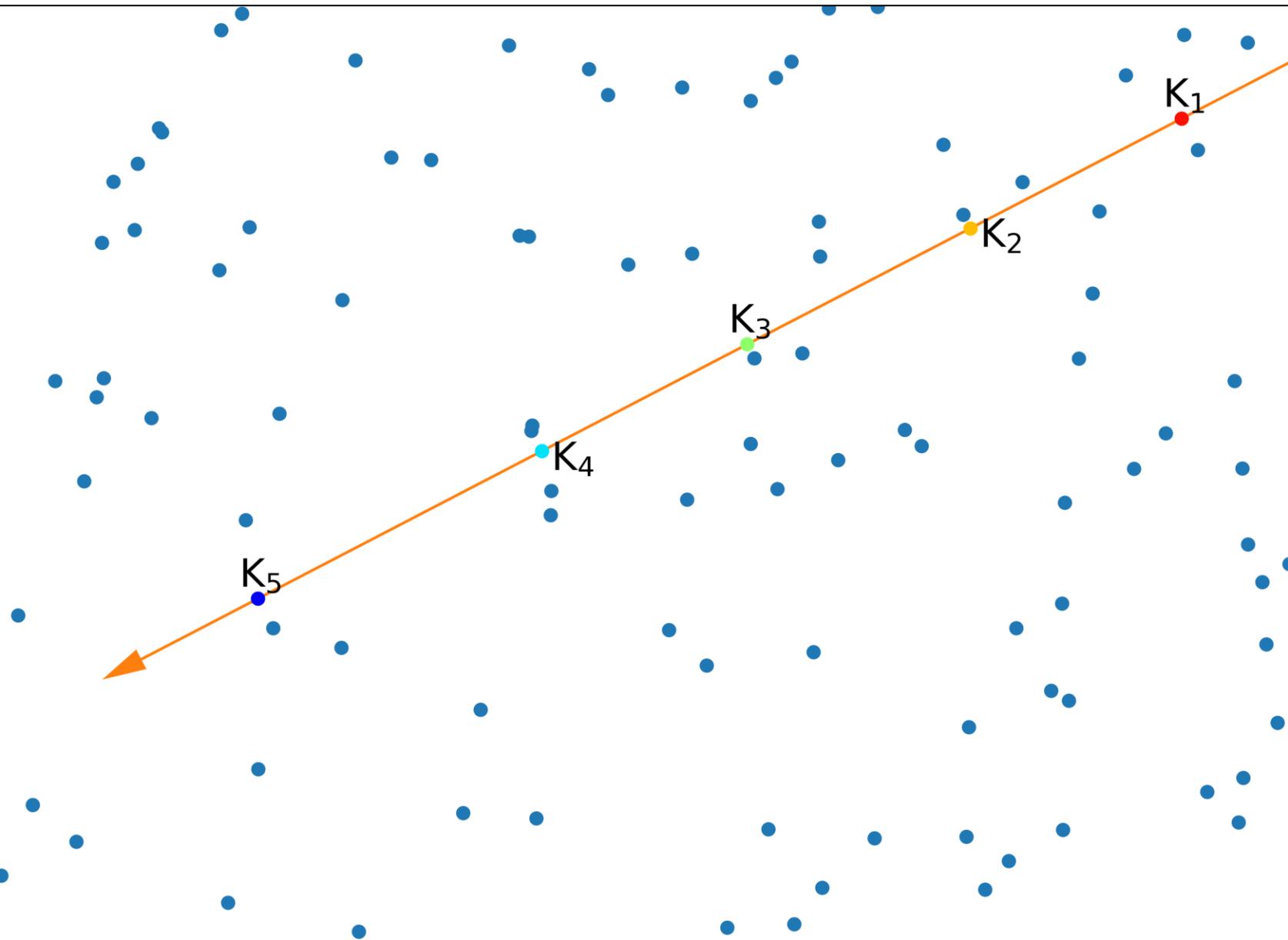
Order 3



Order 2



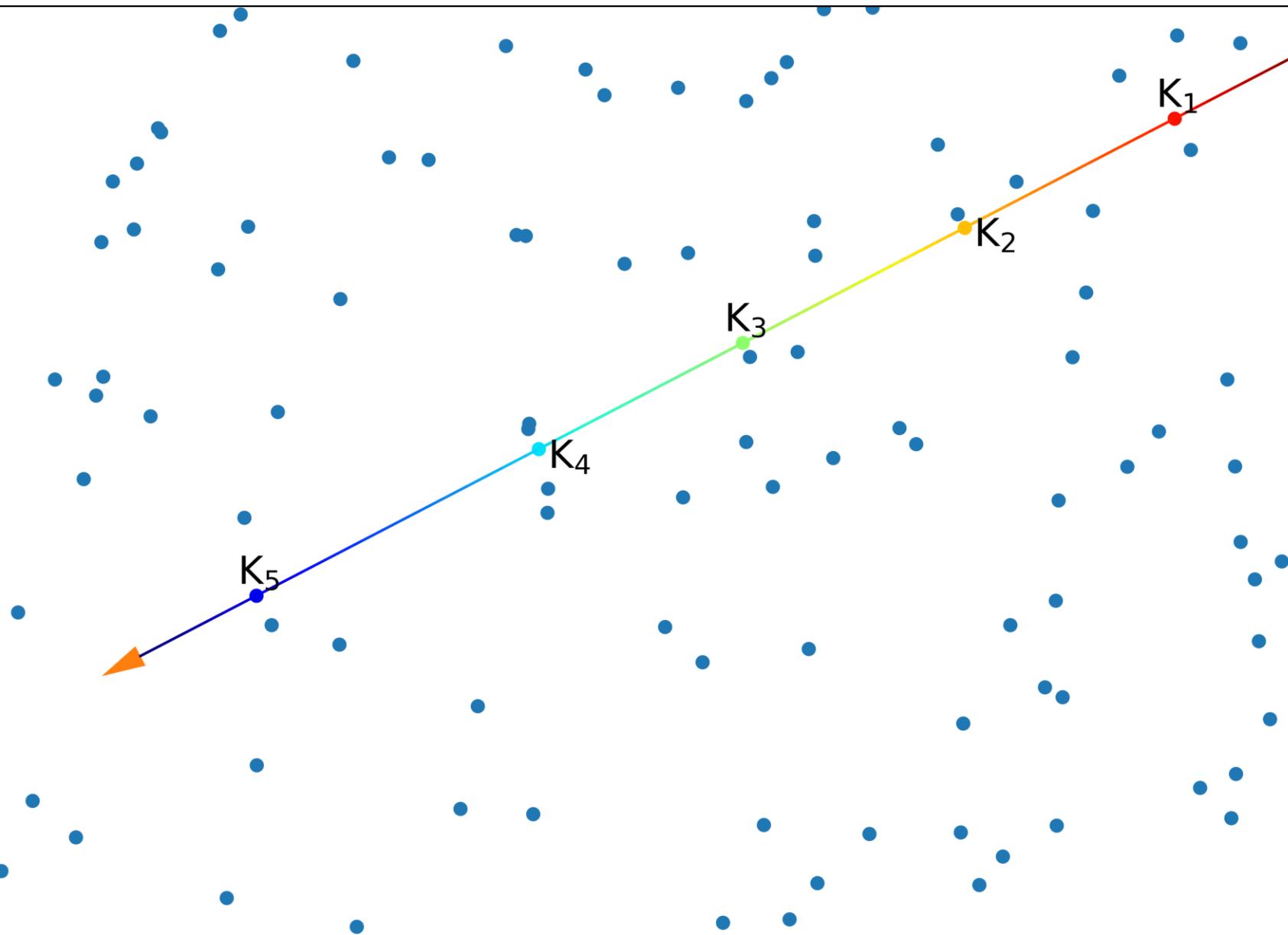
# Interpolation along a ray



At each point K:

- $\tau_i$

# Interpolation along a ray

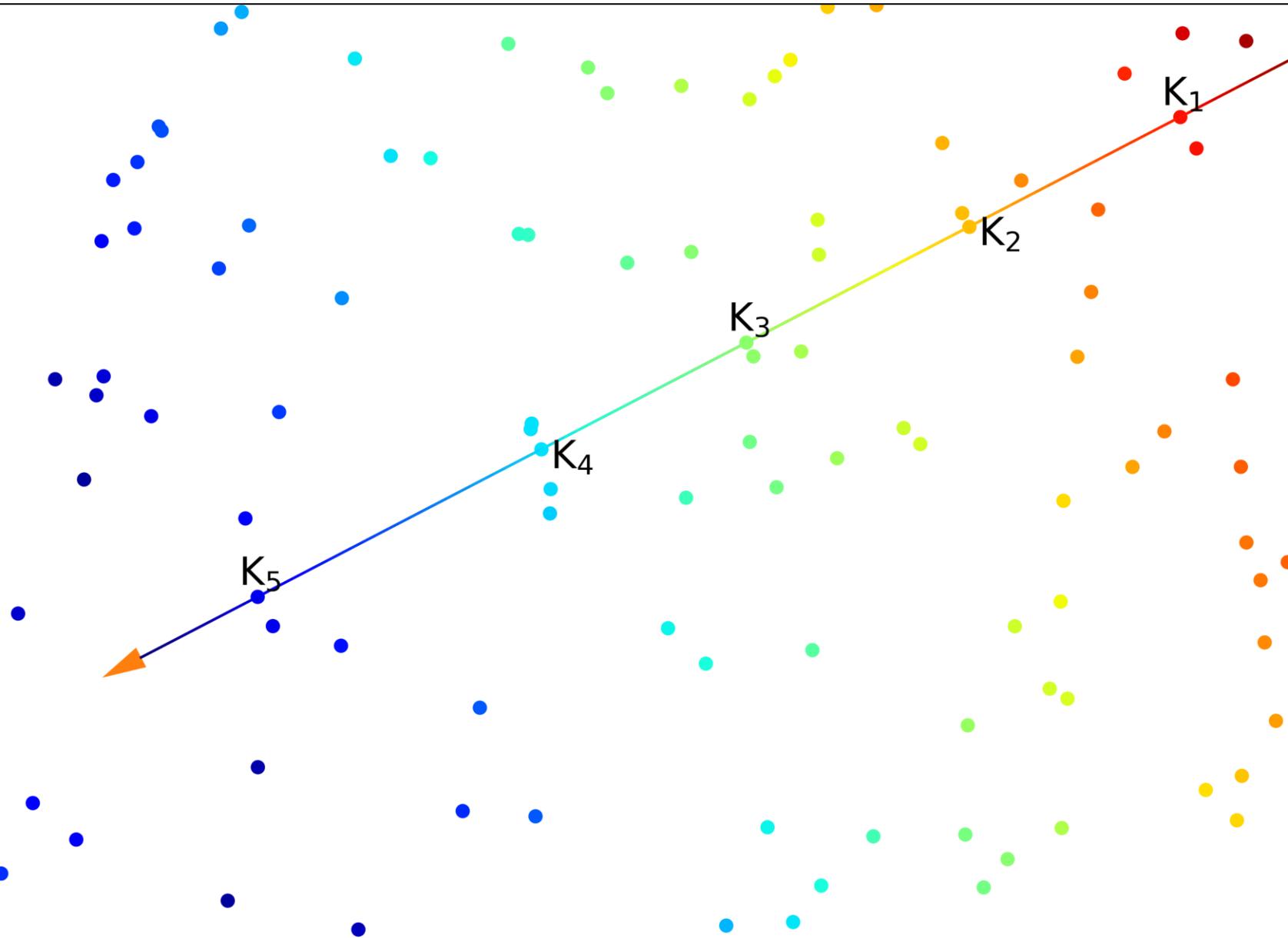


At each point K:

- $\tau_i$

Linear interpolations  
between points

# Interpolation along a ray



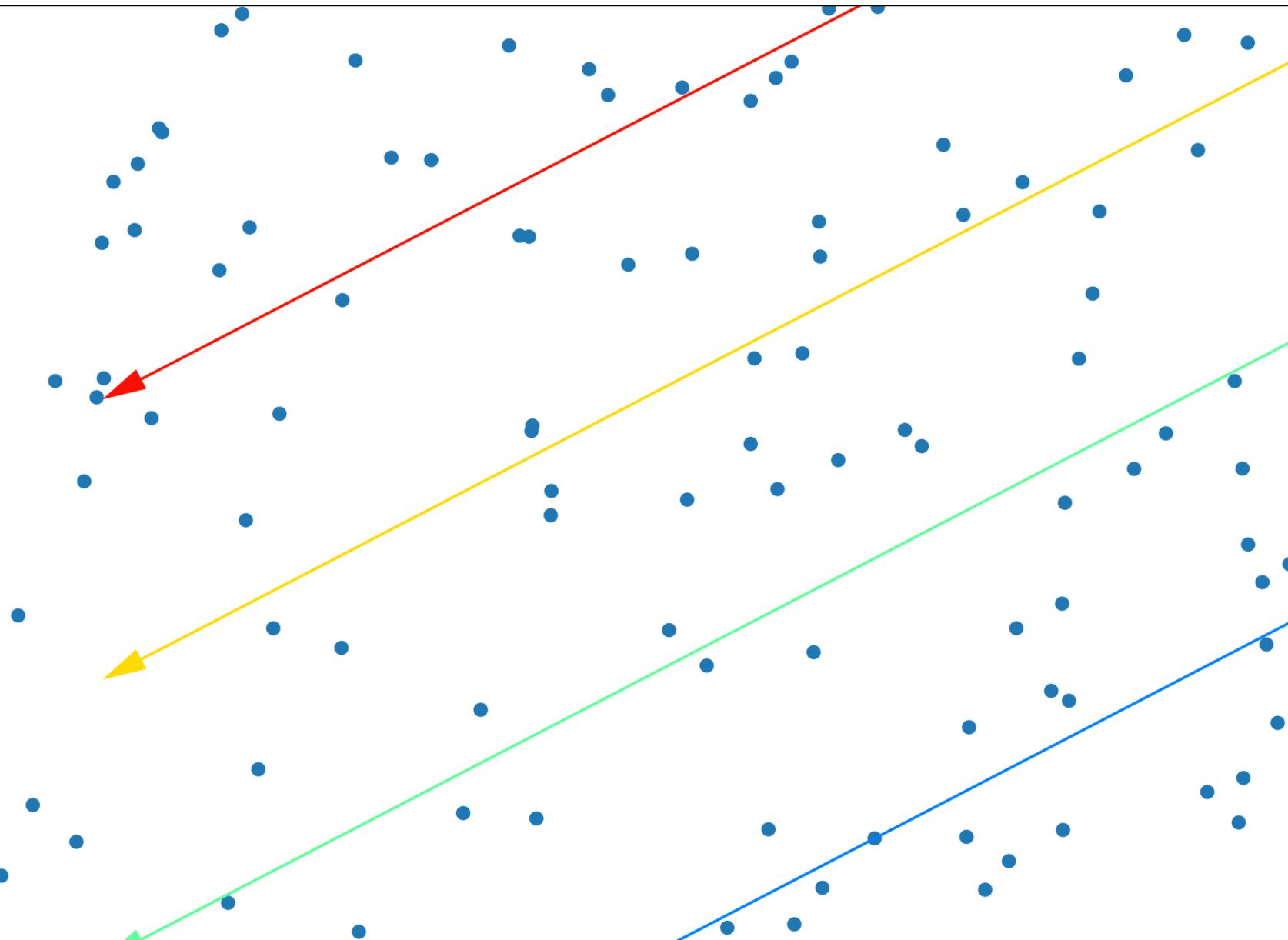
At each point K:

- $\tau_i$

Linear interpolations  
between points

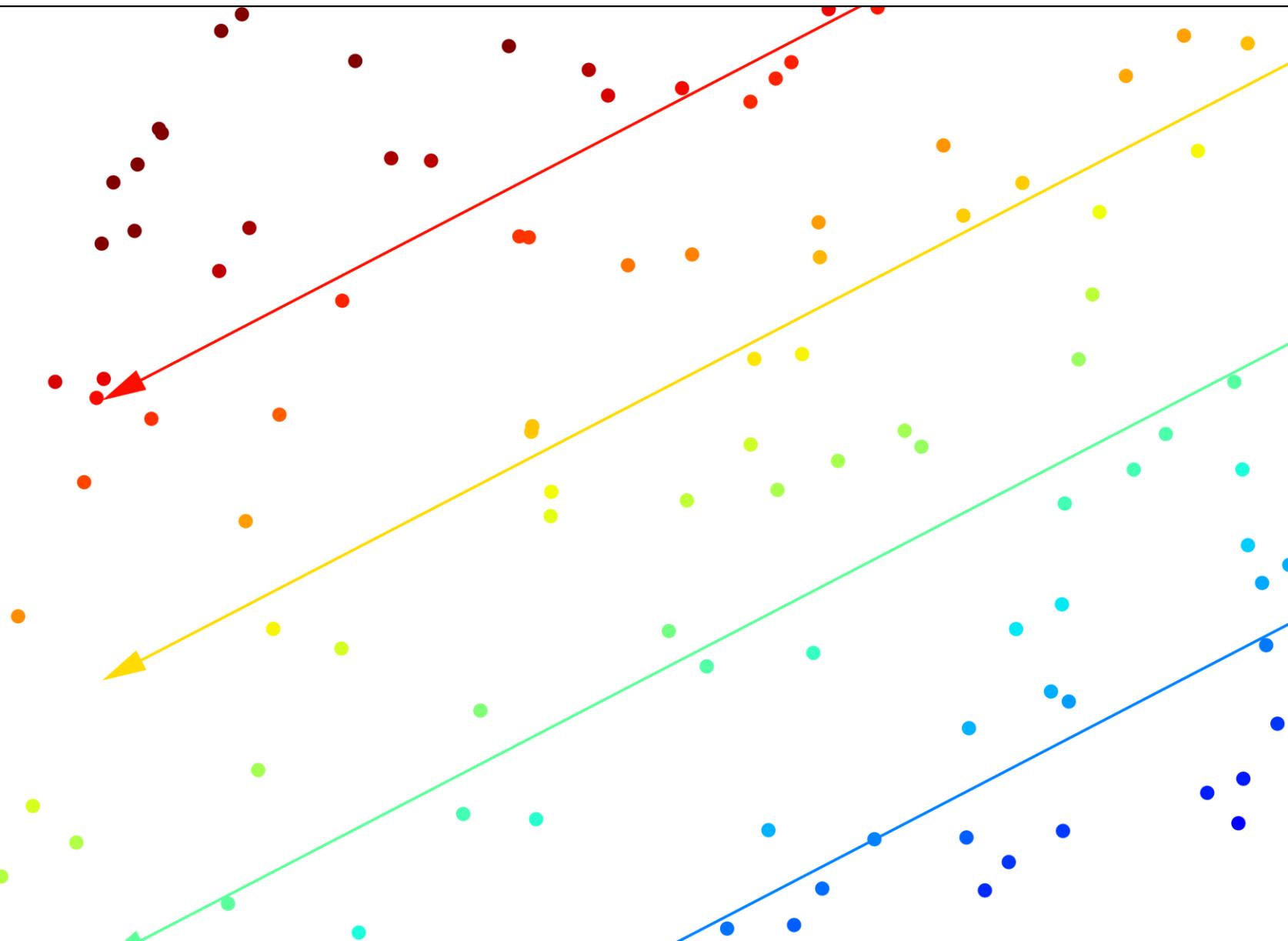
$\tau$  at closest point  
along the ray

# Interpolation in between rays



Trace more rays

# Interpolation in between rays

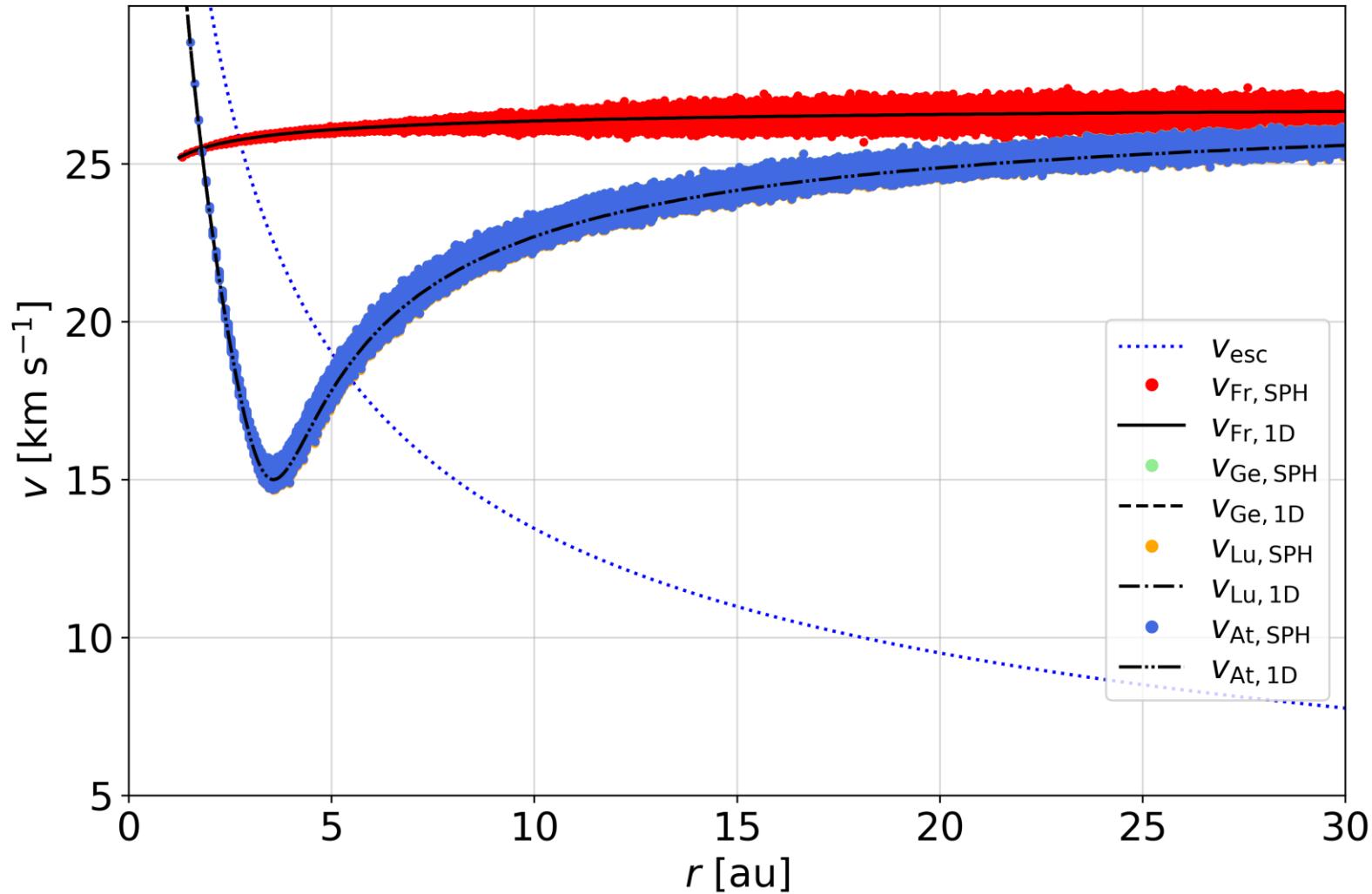


Trace more rays

Interpolate  $\tau$  between  
closest rays

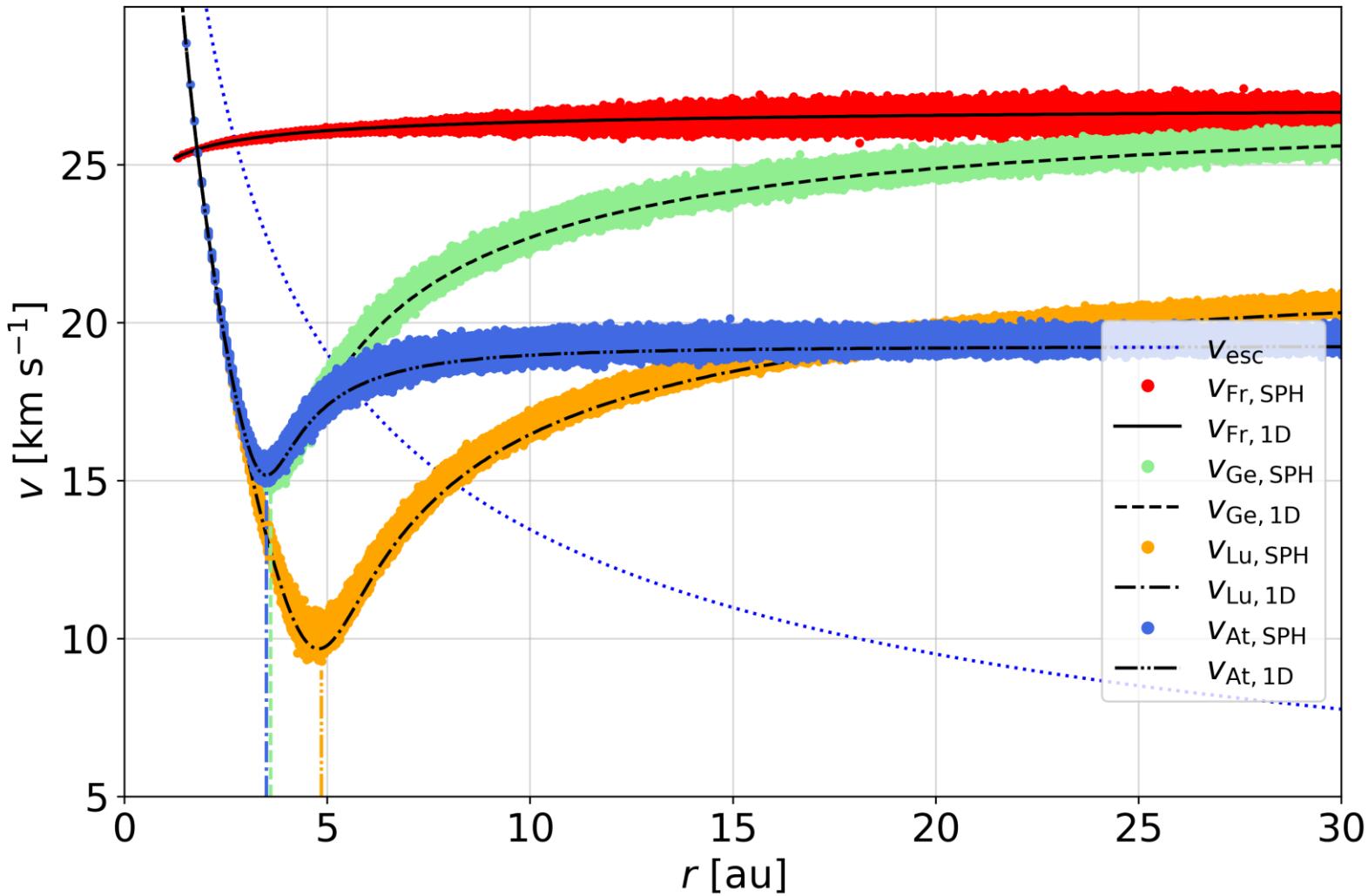
# Velocity profile

Parameter	Value	Unit
$\dot{M}_{\text{AGB}}$	$10^{-8}$ or $3 \times 10^{-6}$	$M_{\odot} \text{ yr}^{-1}$
$M_{\text{AGB}}$	1.02	$M_{\odot}$
$L_{\text{AGB}}$	4384	$L_{\odot}$
$T_{\text{eff,AGB}}$	2874	K
$R_{\text{AGB}}$	1.24	au



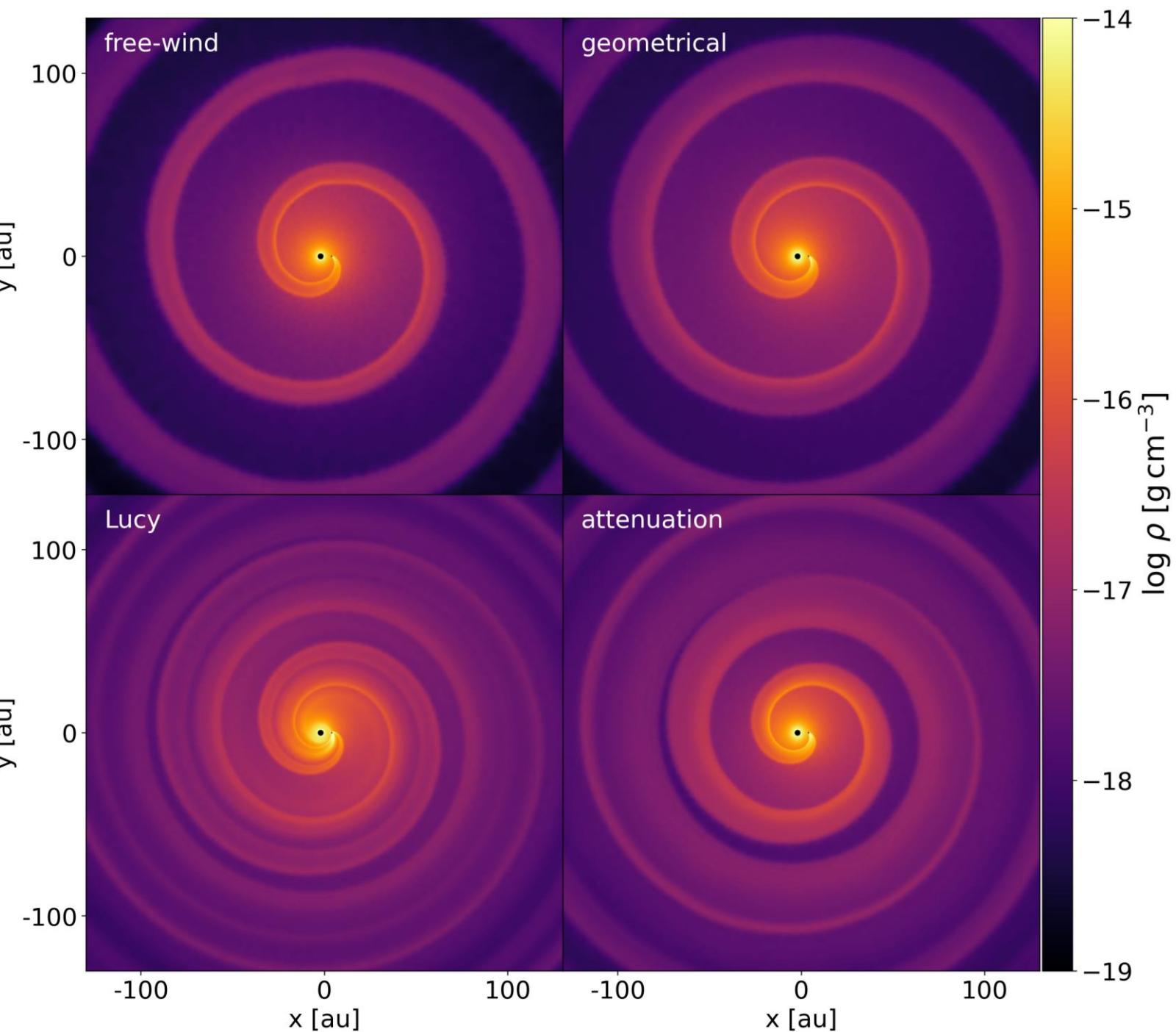
# Velocity profile

Parameter	Value	Unit
$\dot{M}_{\text{AGB}}$	$10^{-8}$ or $3 \times 10^{-6}$	$M_{\odot} \text{ yr}^{-1}$
$M_{\text{AGB}}$	1.02	$M_{\odot}$
$L_{\text{AGB}}$	4384	$L_{\odot}$
$T_{\text{eff,AGB}}$	2874	K
$R_{\text{AGB}}$	1.24	au



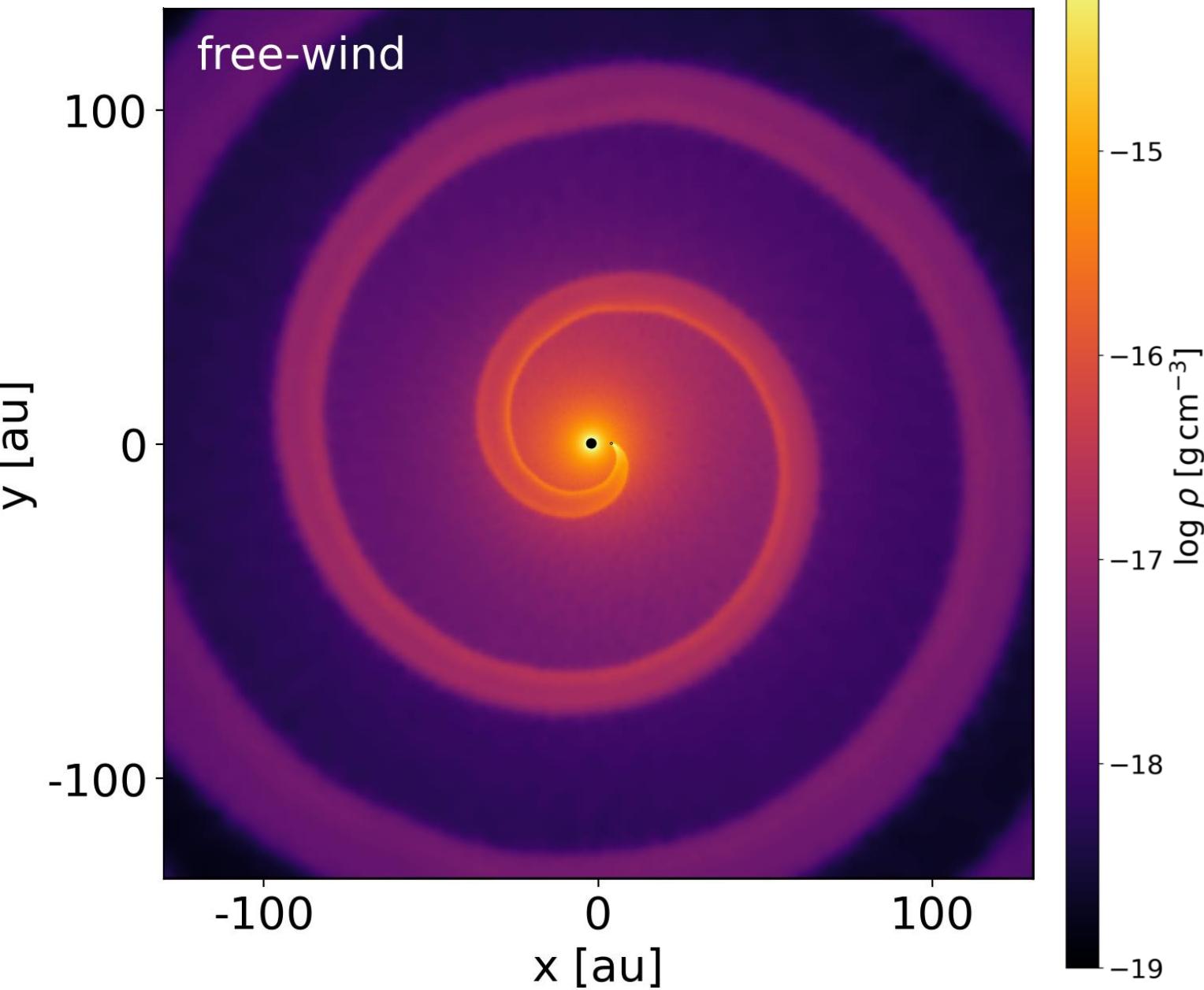
# Morphological structures

Parameter	Value	Unit
$\dot{M}_{\text{AGB}}$	$3 \times 10^{-6}$	$\text{M}_\odot \text{ yr}^{-1}$
$M_{\text{AGB}}$	1.02	$\text{M}_\odot$
$L_{\text{AGB}}$	4384	$\text{L}_\odot$
$T_{\text{eff,AGB}}$	2874	K
$R_{\text{AGB}}$	1.24	au



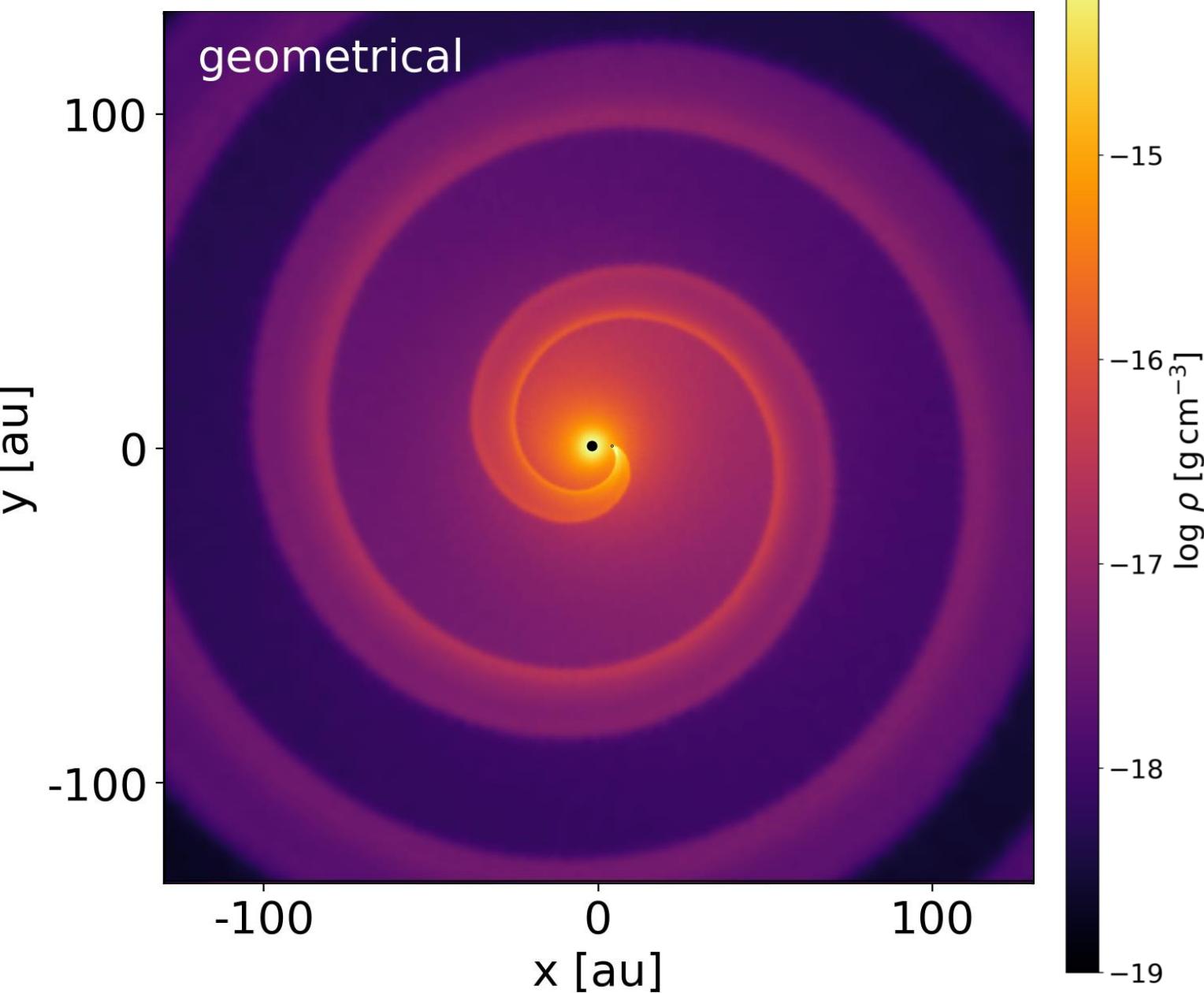
# Morphological structures

Parameter	Value	Unit
$\dot{M}_{\text{AGB}}$	$3 \times 10^{-6}$	$M_{\odot} \text{ yr}^{-1}$
$M_{\text{AGB}}$	1.02	$M_{\odot}$
$L_{\text{AGB}}$	4384	$L_{\odot}$
$T_{\text{eff,AGB}}$	2874	K
$R_{\text{AGB}}$	1.24	au



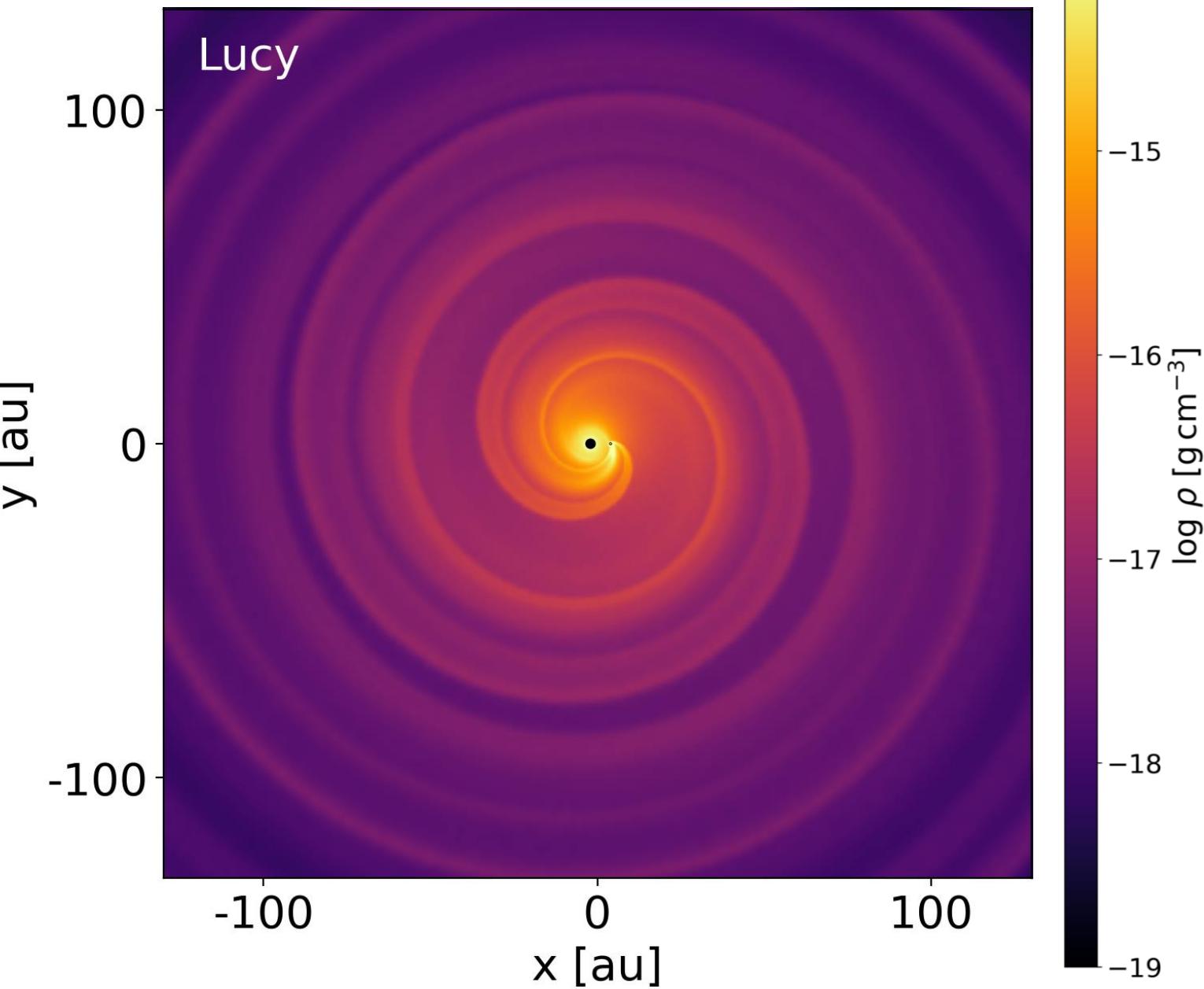
# Morphological structures

Parameter	Value	Unit
$\dot{M}_{\text{AGB}}$	$3 \times 10^{-6}$	$M_{\odot} \text{ yr}^{-1}$
$M_{\text{AGB}}$	1.02	$M_{\odot}$
$L_{\text{AGB}}$	4384	$L_{\odot}$
$T_{\text{eff,AGB}}$	2874	K
$R_{\text{AGB}}$	1.24	au



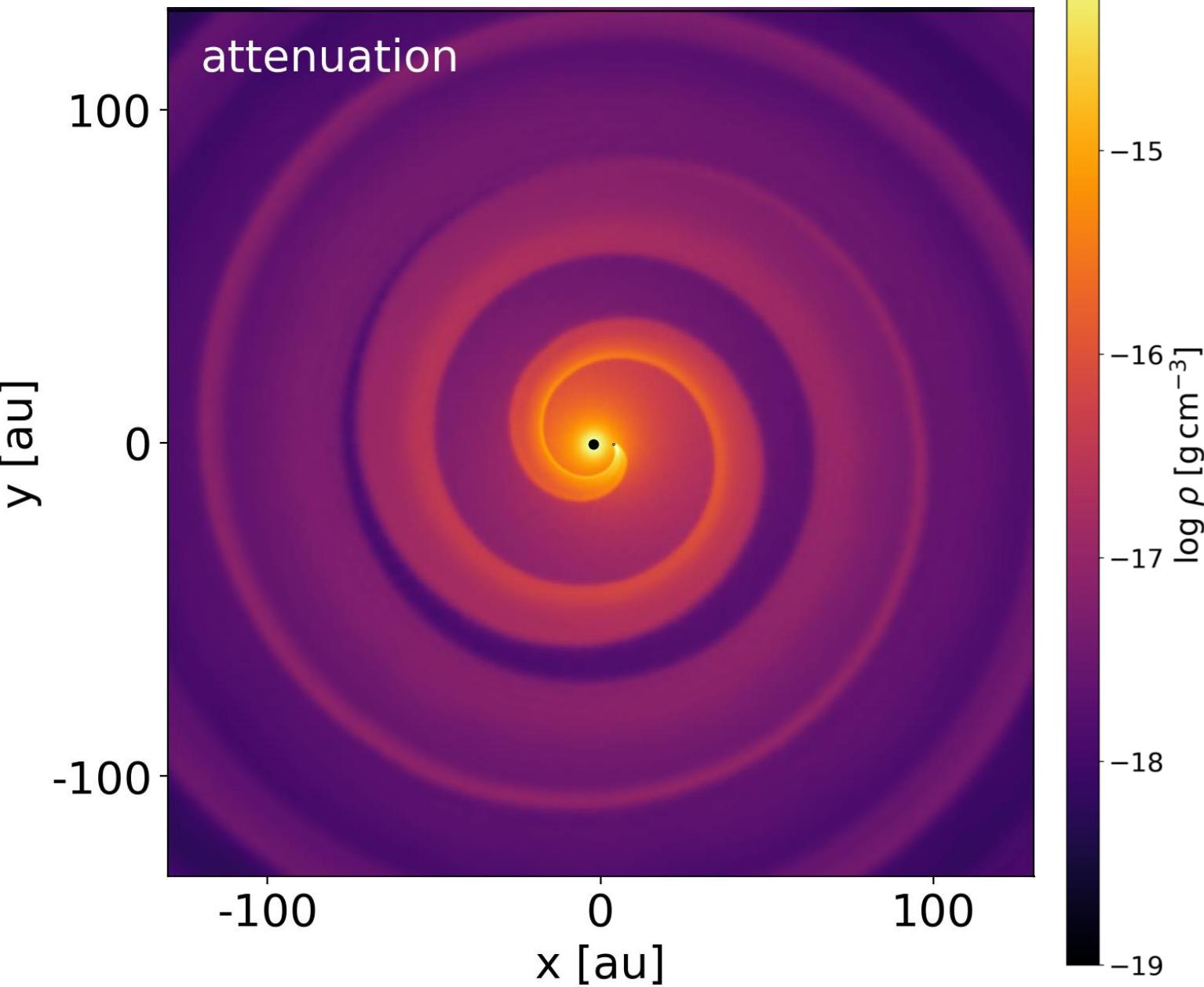
# Morphological structures

Parameter	Value	Unit
$\dot{M}_{\text{AGB}}$	$3 \times 10^{-6}$	$M_{\odot} \text{ yr}^{-1}$
$M_{\text{AGB}}$	1.02	$M_{\odot}$
$L_{\text{AGB}}$	4384	$L_{\odot}$
$T_{\text{eff,AGB}}$	2874	K
$R_{\text{AGB}}$	1.24	au



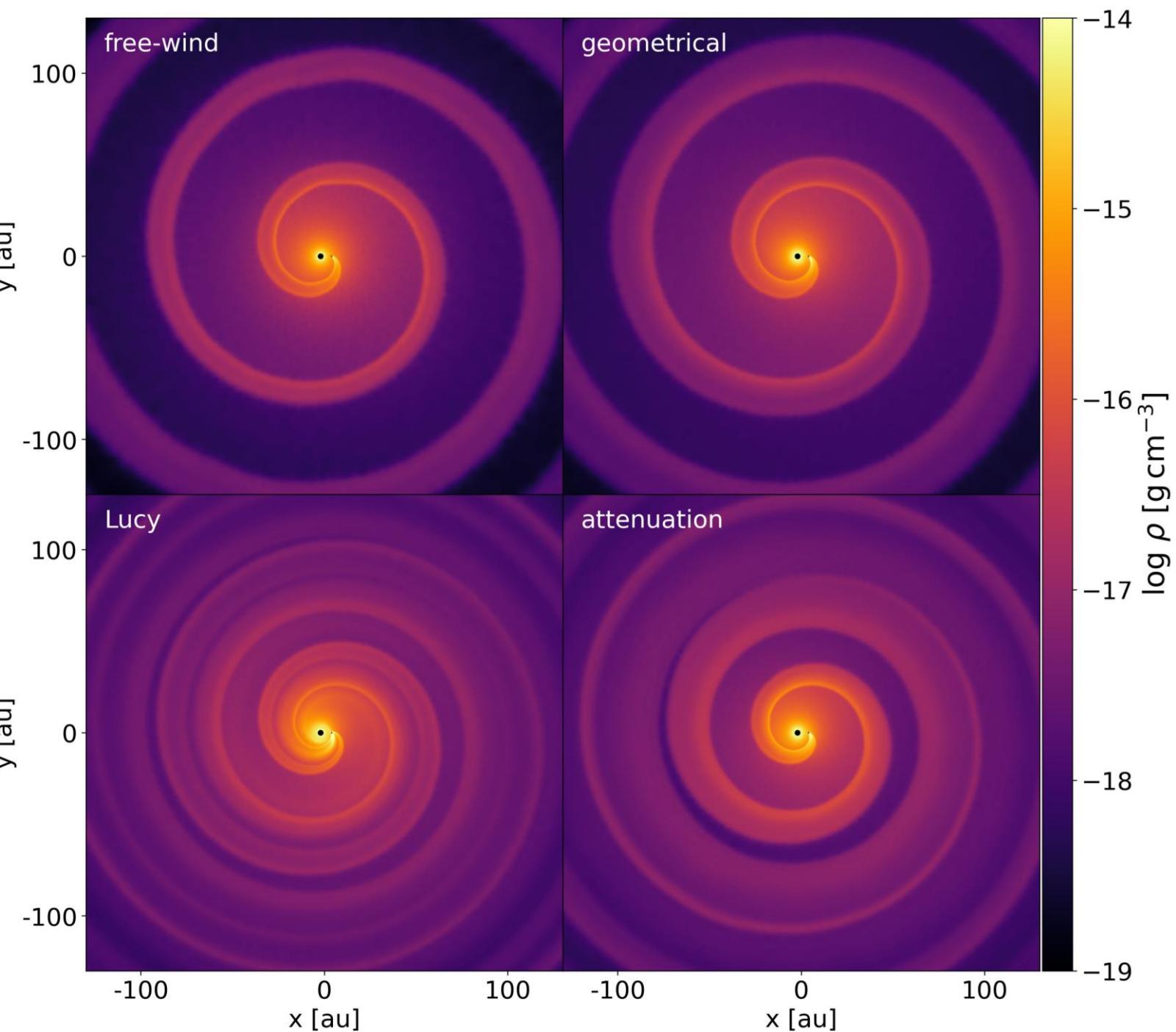
# Morphological structures

Parameter	Value	Unit
$\dot{M}_{\text{AGB}}$	$3 \times 10^{-6}$	$M_{\odot} \text{ yr}^{-1}$
$M_{\text{AGB}}$	1.02	$M_{\odot}$
$L_{\text{AGB}}$	4384	$L_{\odot}$
$T_{\text{eff,AGB}}$	2874	K
$R_{\text{AGB}}$	1.24	au



# Morphological structures

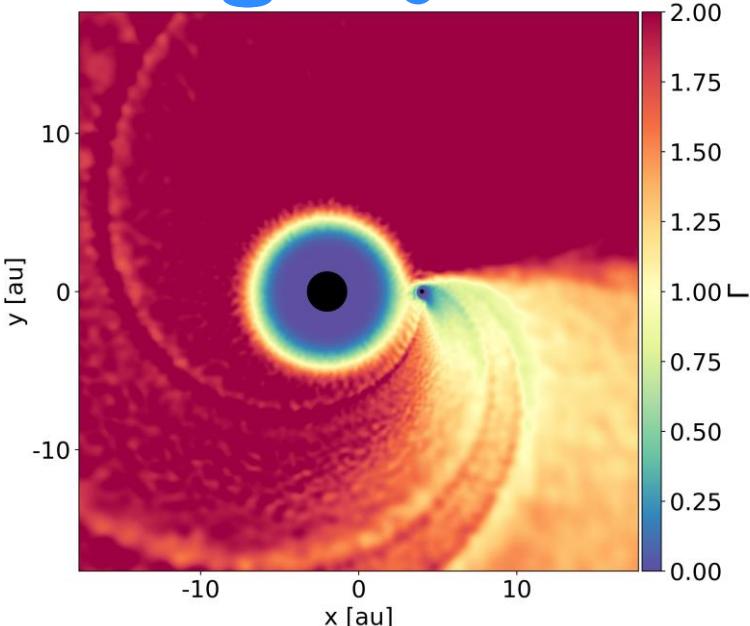
Parameter	Value	Unit
$\dot{M}_{\text{AGB}}$	$3 \times 10^{-6}$	$M_{\odot} \text{ yr}^{-1}$
$M_{\text{AGB}}$	1.02	$M_{\odot}$
$L_{\text{AGB}}$	4384	$L_{\odot}$
$T_{\text{eff,AGB}}$	2874	K
$R_{\text{AGB}}$	1.24	au



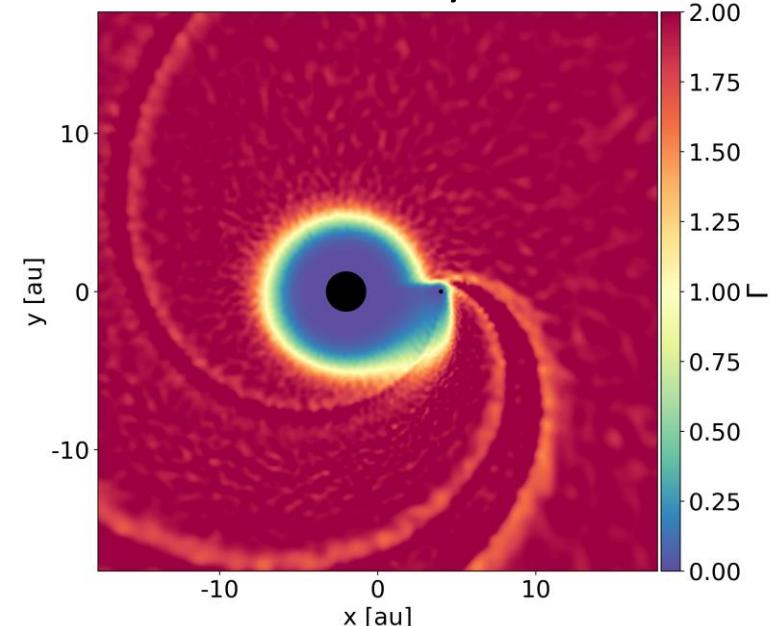
# Validation Study

- Full 3D radiation transfer code  
Magritte
- Lucy  
approximation  
most accurate

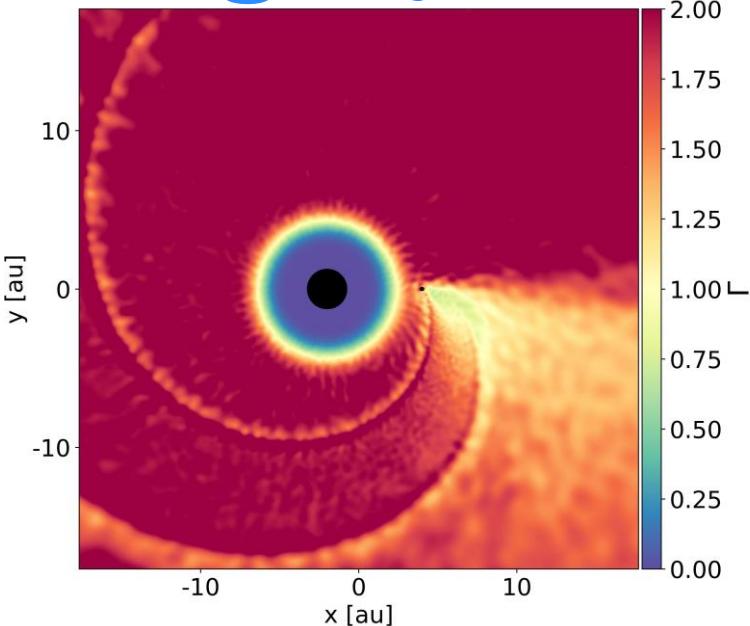
Magritte



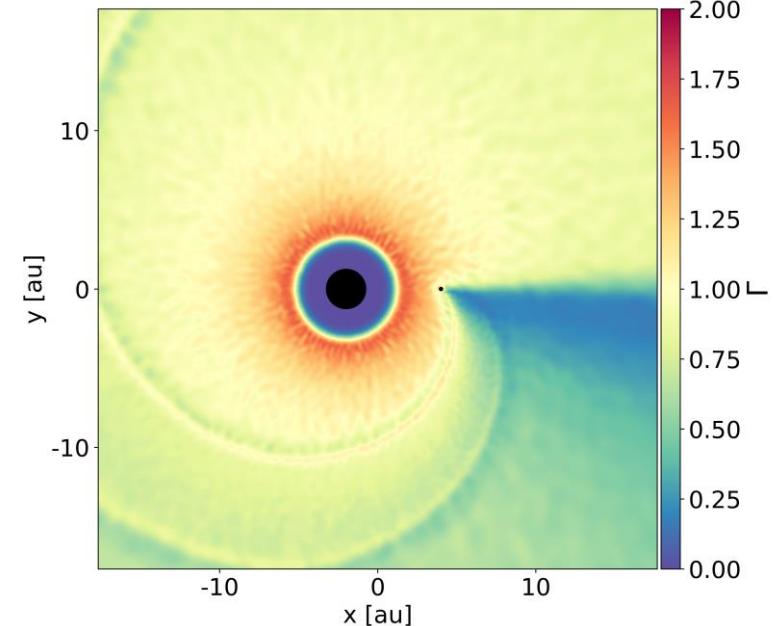
Lucy



Magritte

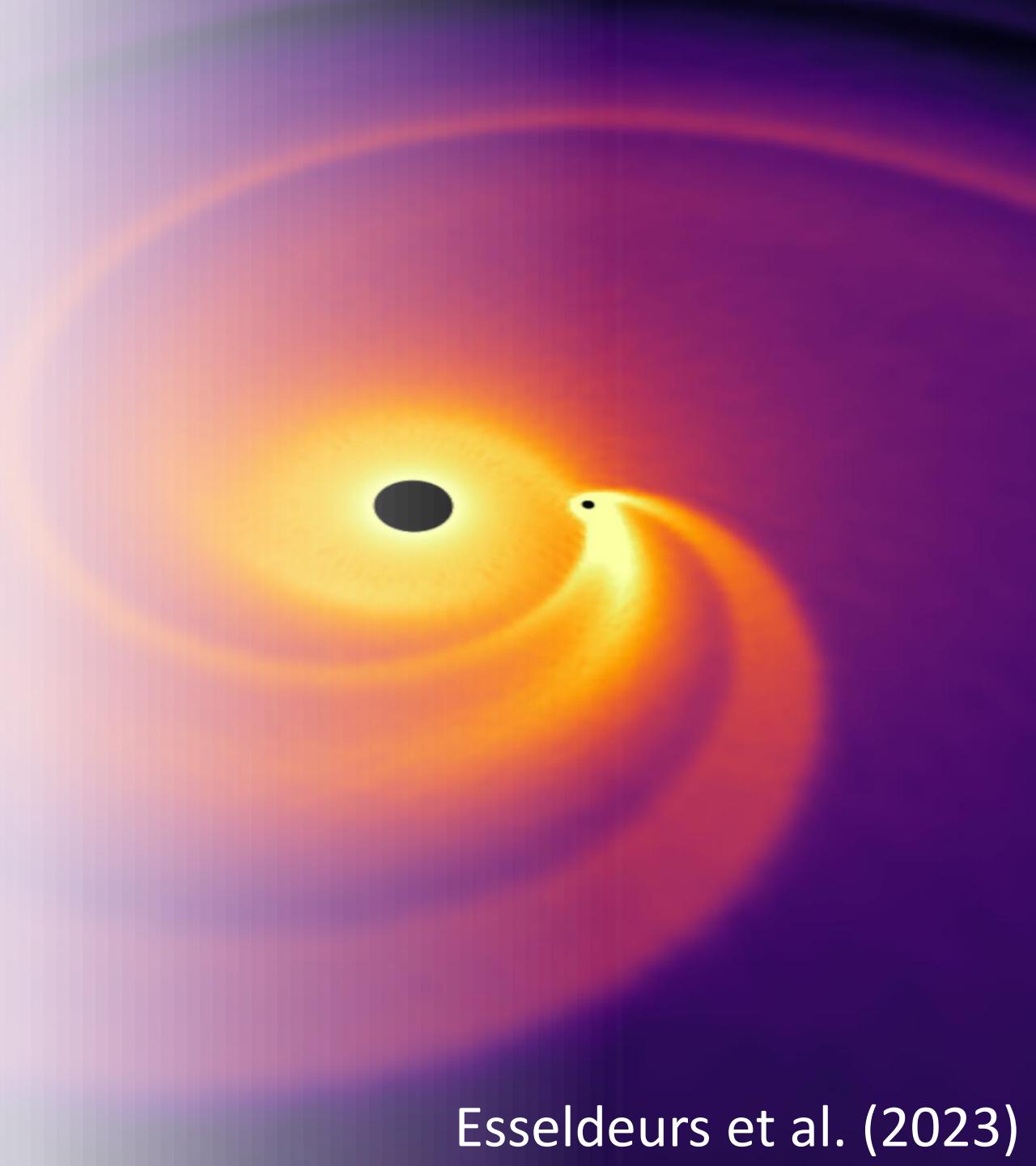


Attenuation



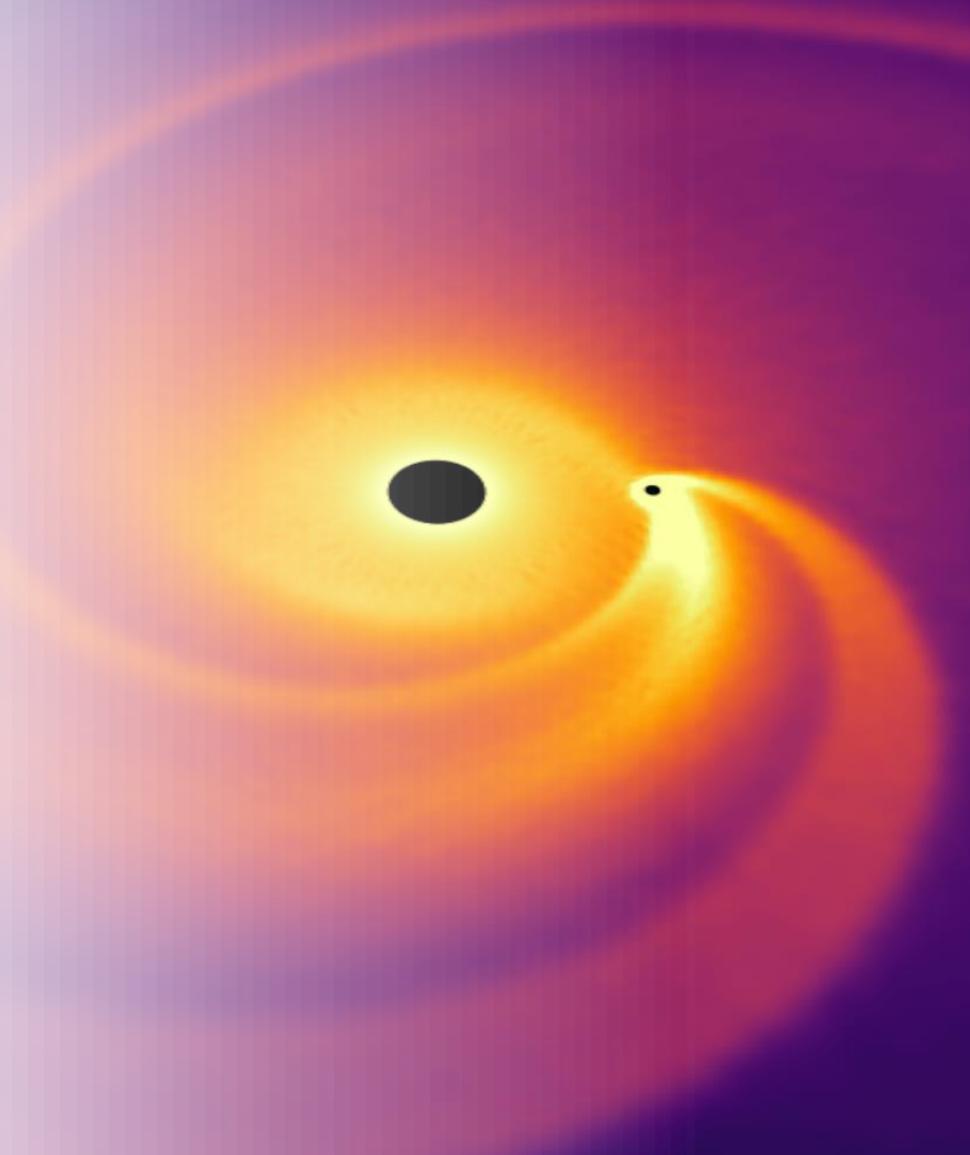
# Conclusions

- Dust formation and radiative transfer is crucial
- Different approximations can make significant changes
- Lucy approximation most accurate



# Future work

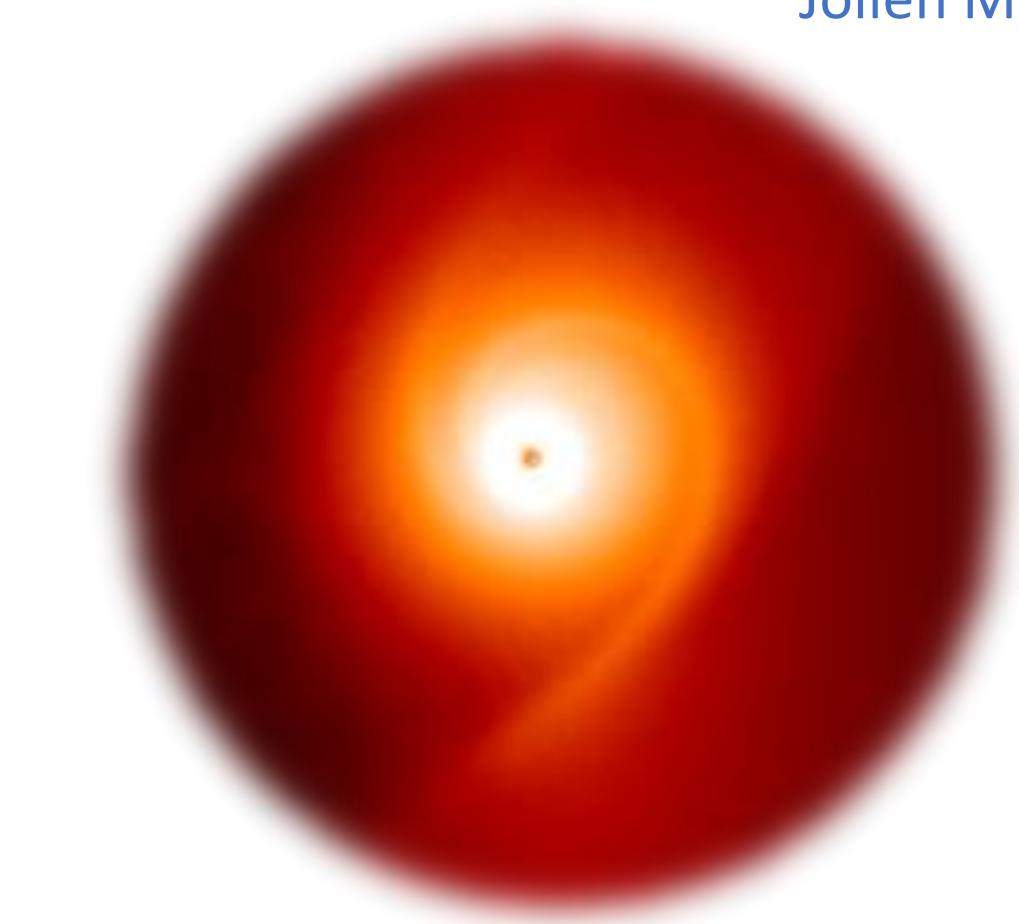
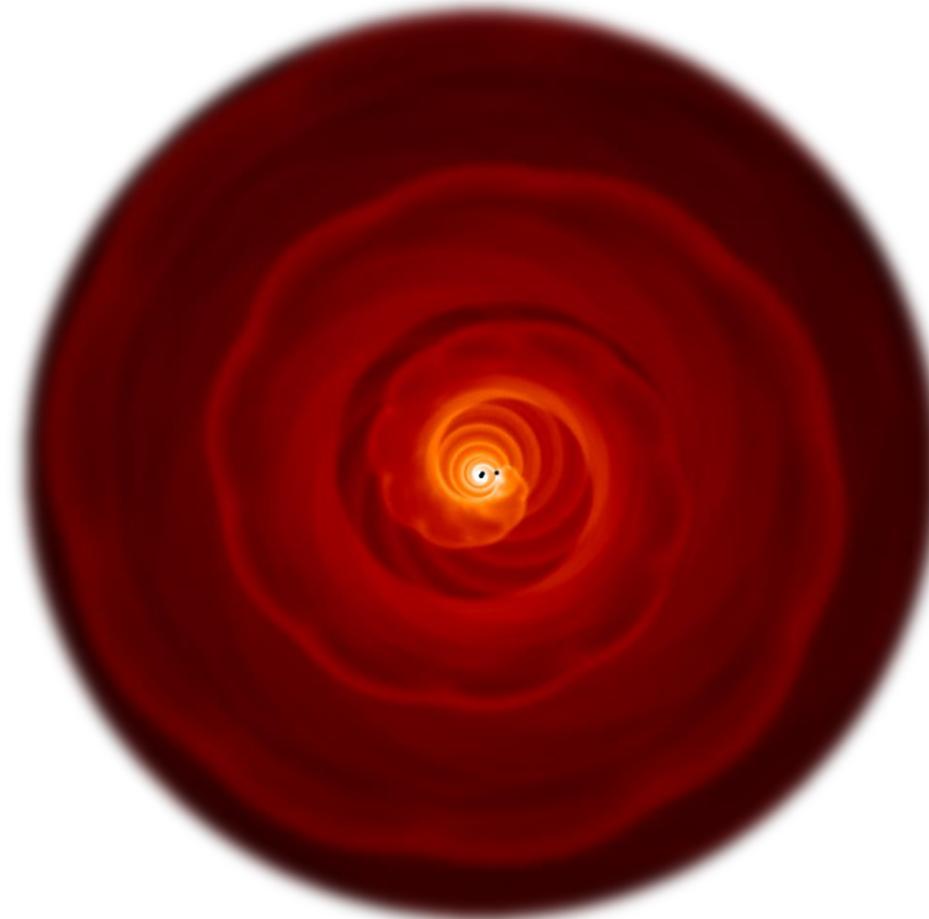
- Combination of Lucy and attenuation approximation
- Couple Phantom to MCFOST for full radiation transfer calculation



# Tripple simulations and disk formation

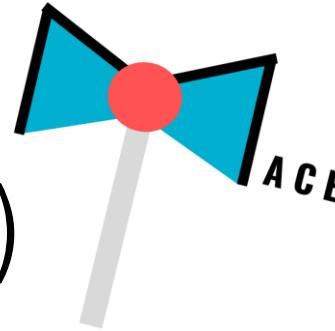


Jolien Malfait

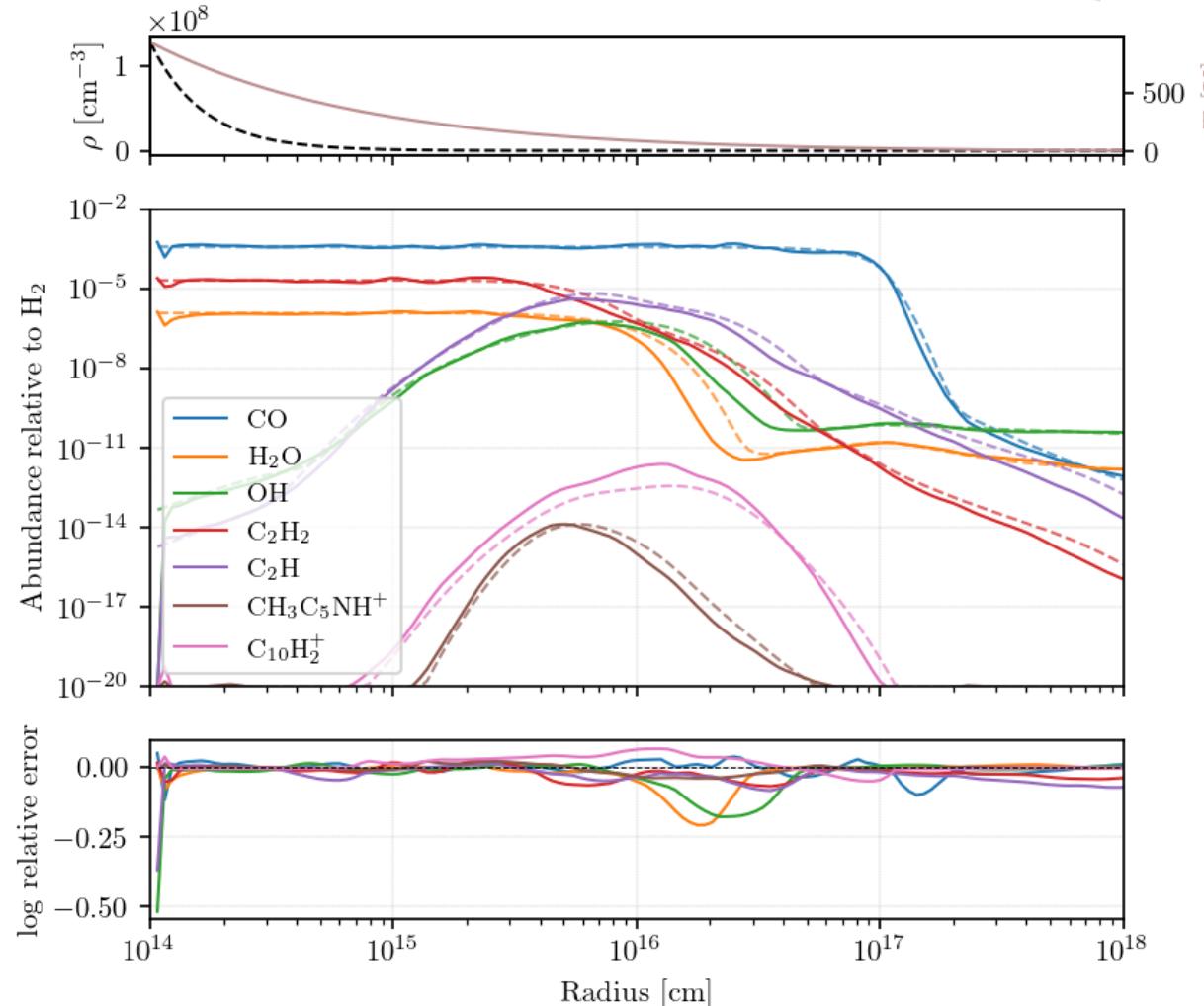


Malfait+ (in prep. a,b)

# Machine learning Approach to Chemistry Emulation (MACE)



Silke Maes



Maes+ (in prep.)

# AMUSE



Steven Rieder



# Magritte

- Open-source software library for  
**3D non-LTE line radiative transfer**

De Ceuster+ (2020a,b; 2022), Ceulemans+ (in prep.),  
[github.com/Magritte-code/Magritte](https://github.com/Magritte-code/Magritte)



Thomas  
Ceulemans

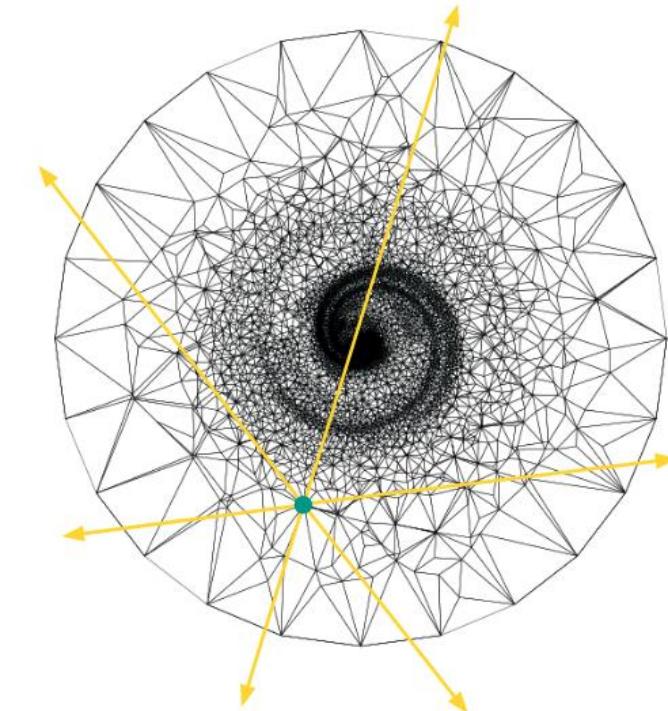


Frederik De  
Ceuster

- **Optimize discretization** for RT through remeshing  
(De Ceuster+ 2020b & accelerated by Ceulemans+ in prep.)
- **Traces rays and solves RT equation** along each ray
- **GPU version** in progress



Magritte<sub>torch</sub>



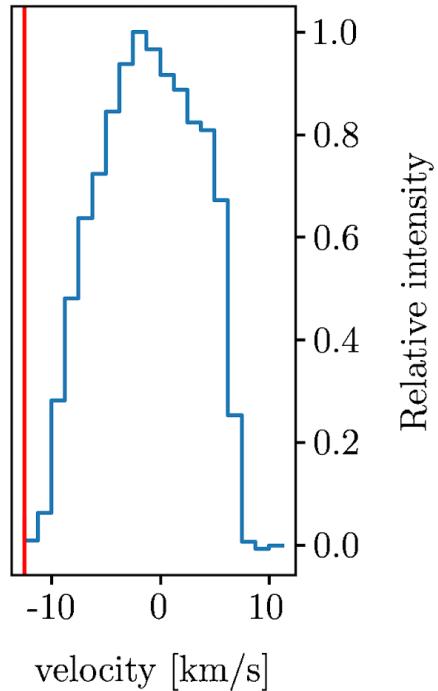
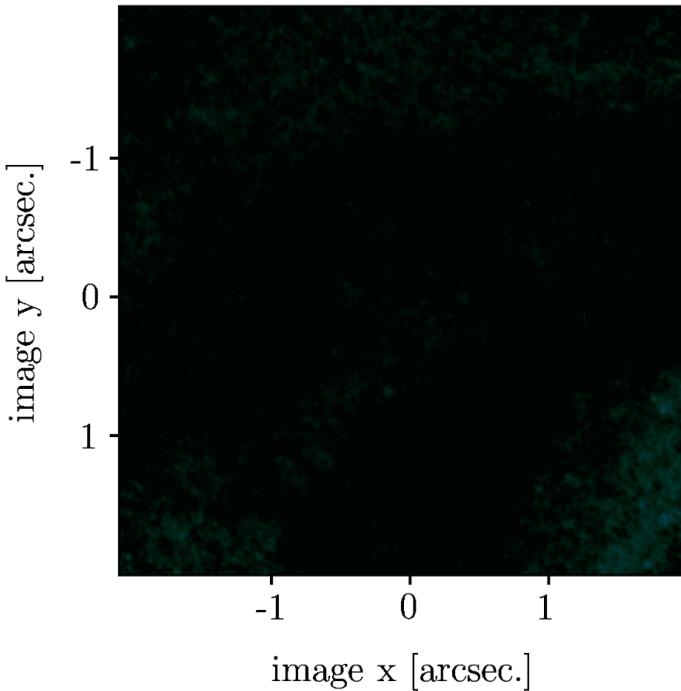


# Magritte

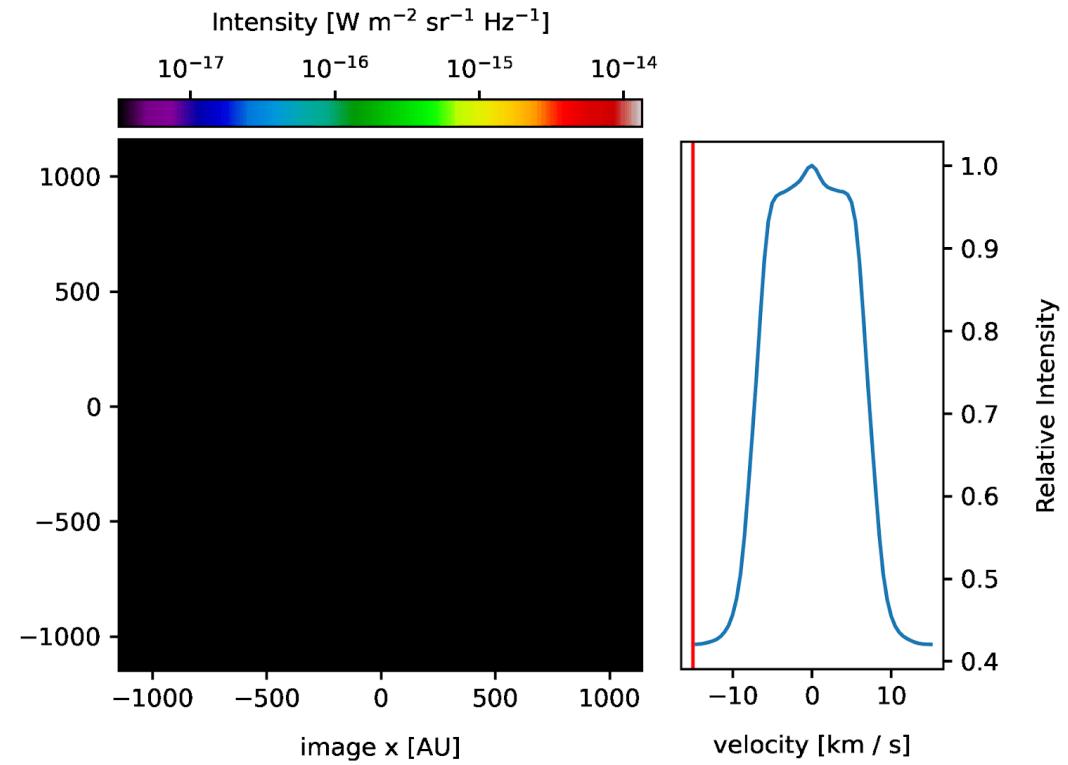


Jolien Malfait

R Aql observation

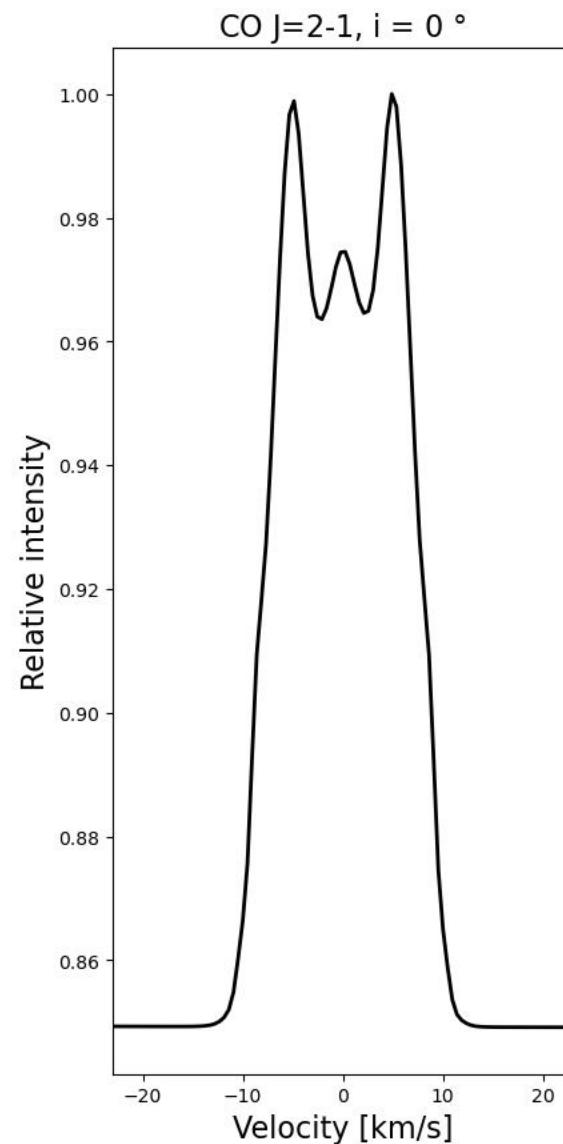
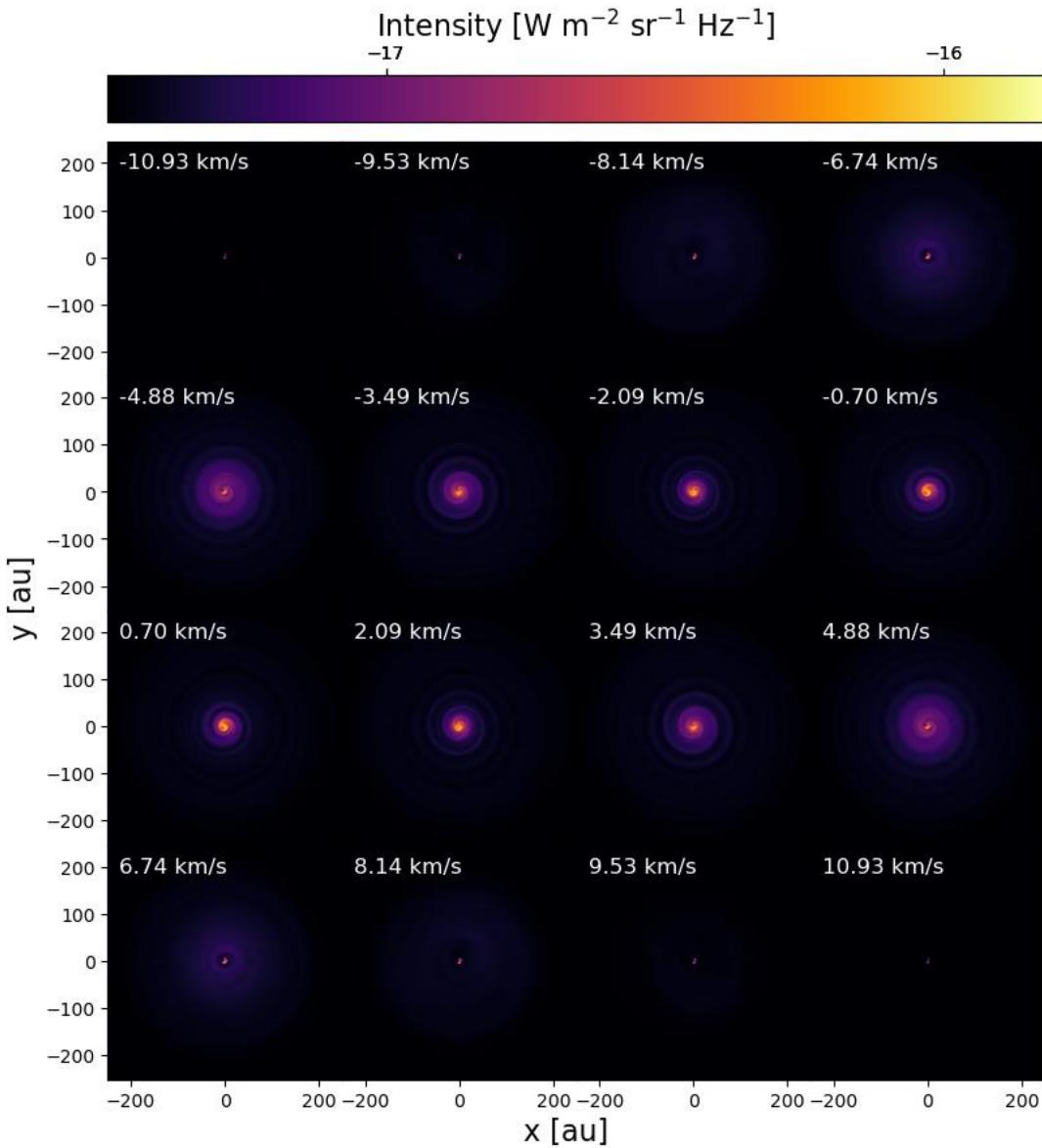


Triple system synthetic observations





# Magritte



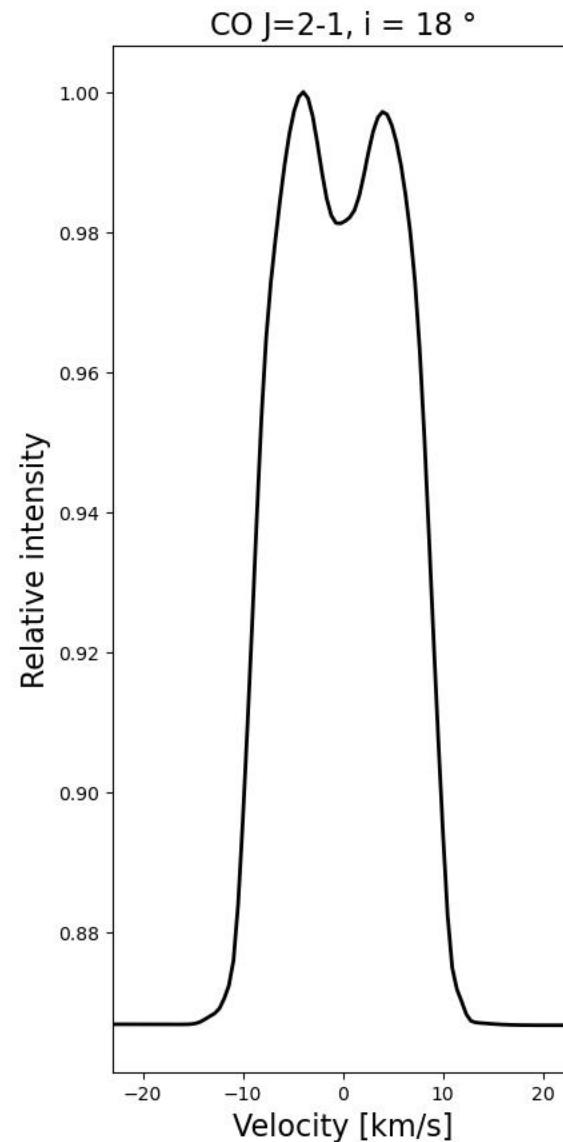
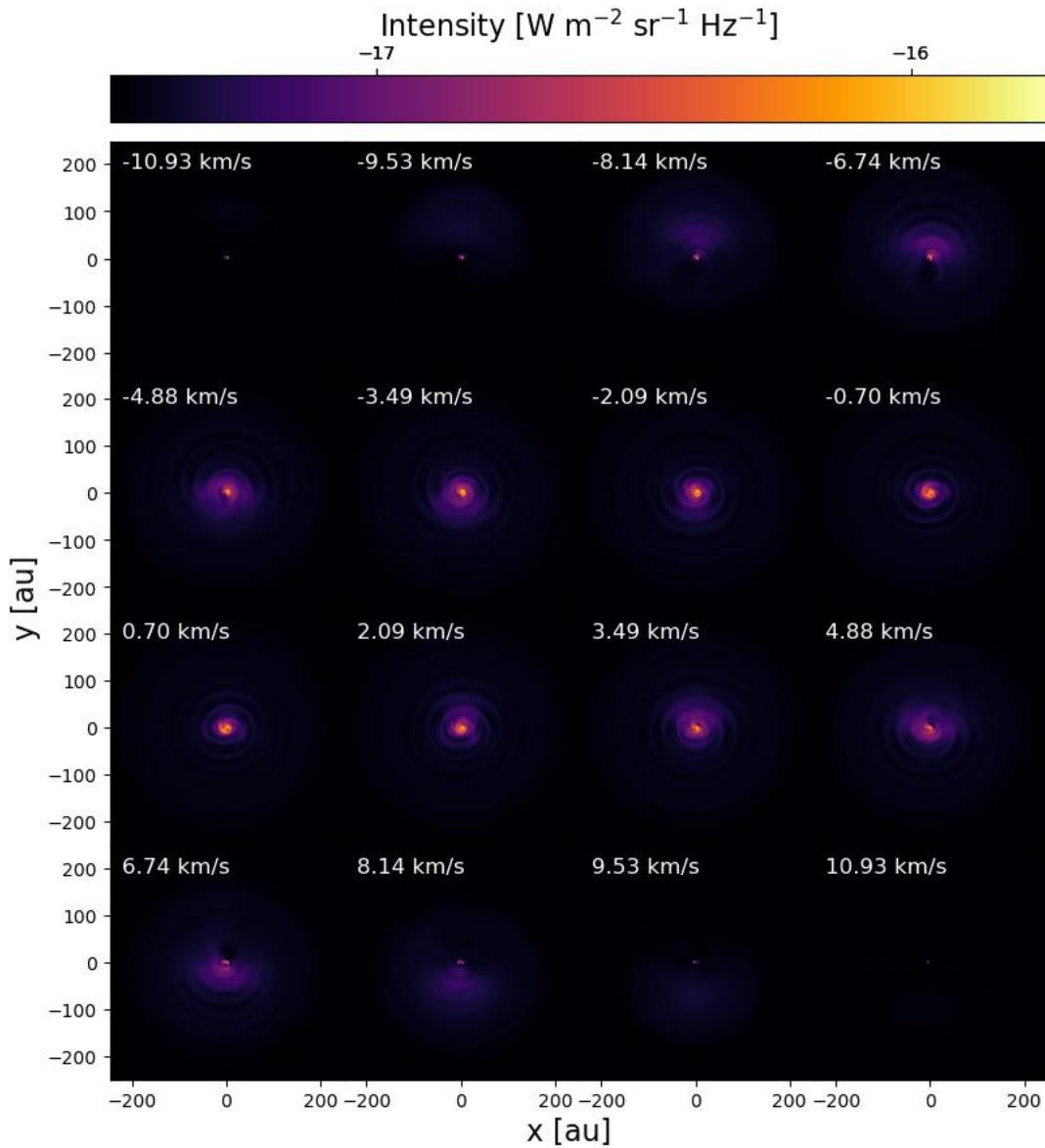
Jolien Malfait



Owen  
Vermeulen



# Magritte



Jolien Malfait

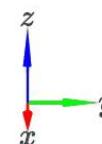
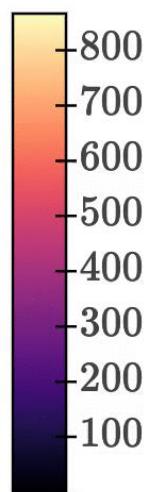
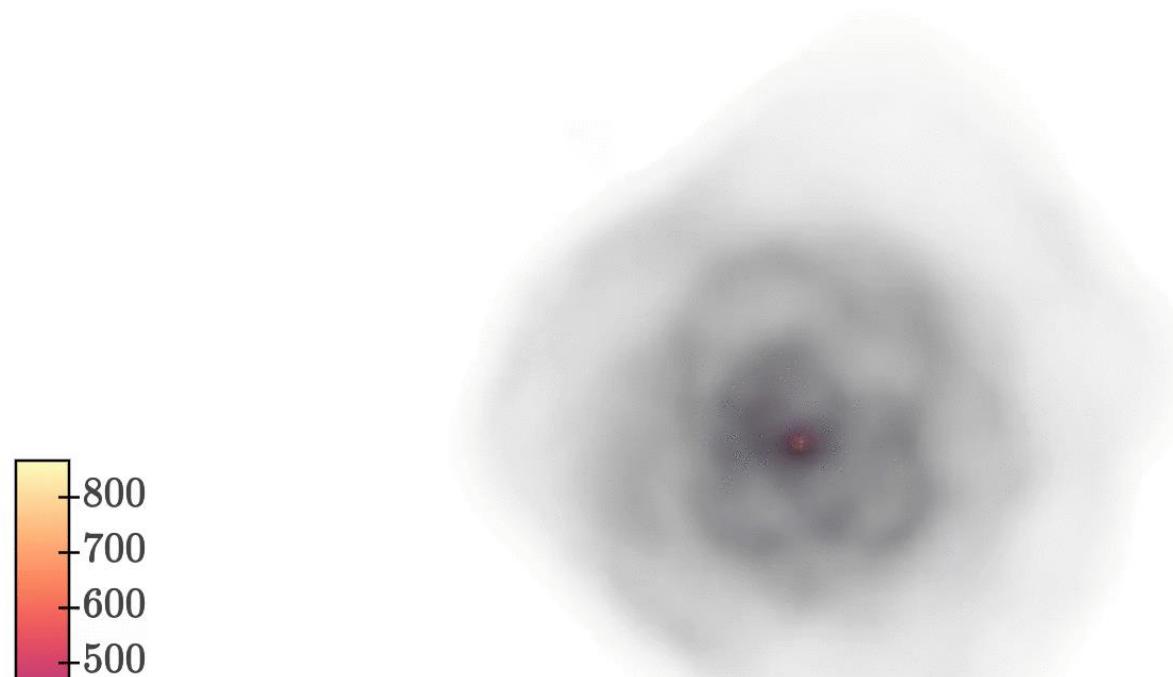


Owen  
Vermeulen

# p3droslo



Frederik De  
Ceuster



De Ceuster+ (in prep.)